Vibrational dynamics of CO⁺ in intense laser fields

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Overview

Motivation: Study nuclear vibrational motion of CO^+ and interaction of CO with laser pulses at femtosecond time scales

Outline:

- Experimental methods and prior results
- ▶ Theoretical methods
- Preliminary theoretical calculations
- ▶ Simulated experiment and results

Pump-probe spectroscopy

Pump-probe spectroscopy provides an experimental method to study vibrational nuclear motion:



1. Ionization from neutral ground state by pump pulse $\Psi_{\text{gr.}} \rightarrow \sum_{\nu} \alpha_{\nu} \psi_{\nu} e^{-i\omega_{\nu}t}$

Pump-probe spectroscopy

Pump-probe spectroscopy provides an experimental method to study vibrational nuclear motion:



- 1. Ionization from neutral ground state by pump pulse
- 2. Wavepacket oscillation and dephasing

Pump-probe spectroscopy

Pump-probe spectroscopy provides a way to study vibrational nuclear motion:



- 1. Ionization from neutral ground state by pump pulse
- 2. Wavepacket oscillation and dephasing
- 3. Dissociation by probe pulse and imaging

Previous CO⁺ experimental results



 \blacktriangleright 800 nm, ~8 fs, 3×10^{14} W / cm² laser pulses

▶ Up to 2 ps delay between pulses

¹De S., et al., 2011

Numerical method

 Numerically integrate the one-dimensional time-dependent Schrodinger equation:

$$\frac{\partial}{\partial t}\Psi\left(\vec{r},t\right) = -i\hat{\mathbf{H}}\Psi\left(\vec{r},t\right)$$

• Approximate solution over small time steps:

$$\Psi\left(\vec{r},t+\Delta t\right)=e^{-i\hat{\mathbf{H}}(t)\Delta t}\Psi\left(\vec{r},t\right)$$

 Cayley / Crank-Nicholson approximation on a numerical internuclear grid:

$$\Psi\left(\vec{r},t+\Delta t\right) = \frac{1-i\hat{\mathrm{H}}\left(t+\frac{\Delta t}{2}\right)\frac{\Delta t}{2}}{1+i\hat{\mathrm{H}}\left(t+\frac{\Delta t}{2}\right)\frac{\Delta t}{2}}\Psi\left(\vec{r},t\right) + \mathcal{O}\left(\Delta t^{3}\right)$$

$\rm CO^+$ molecular potential curves

 $\rm CO^+$ potential curves were digitized from existing literature²



- ▶ 15 fs. laser pulses, up to 2 ps. delay between pulses
- ► Coupled X²Σ⁺, A²Π, and B²Σ⁺ CO⁺ states with C²∆ state for probe pulse
- ► Electronic dipole couplings calculated with GAMESS quantum chemistry software

²Okada, K. et al., 2000

Single cation curve calculations





- Ionization using Franck-Condon transition
- Field-free propagation in excited CO⁺ state
- ► Time evolution of |Ψ|² shows vibrational dephasing and revival

Preliminary single curve calculations



Frequency

- Ionization using Franck-Condon transition
- ▶ Field-free propagation in excited CO⁺ state
- Power spectra shows beat frequencies of vibrational energy levels

Single curve calculation example - ${\rm A}^2\Pi$



- Gives information on nuclear dynamics within molecular orbital
- Provides reference for checking more complicated simulation results
- Potential curve mapping from power spectra

Dipole-coupled calculations

- Simulated simplified pump-probe spectroscopy experiment with transitions to / from coupled binding and dissociative molecular orbitals
- Dipole-coupled propagation:

$$\frac{\partial}{\partial t} \begin{pmatrix} \Psi_1 \\ \Psi_2 \end{pmatrix} = -i \begin{pmatrix} \hat{\mathbf{T}} + \hat{\mathbf{V}}_1 & \hat{\mathbf{D}}_{1,2} \\ \hat{\mathbf{D}}_{2,1} & \hat{\mathbf{T}} + \hat{\mathbf{V}}_2 \end{pmatrix} \begin{pmatrix} \Psi_1 \\ \Psi_2 \end{pmatrix}$$
$$\hat{D}_{i,j} = E(t) \langle \Psi_i \mid R \mid \Psi_j \rangle$$

- Interested in dissociated portion of wavepacket after probe pulse
- Manually locate a "cutoff distance" R_c that distinguishes bound and dissociative nuclear motion

Dipole-coupled calculations

 Obtain kinetic energy release (KER) from momentum representation (Fourier transform) of dissociative wavepacket:

$$\tilde{\Psi}_{\text{Diss.},i}\left(P,t\right) = \int_{R_{c}}^{R_{max}} \Psi_{i} e^{-iPR} dR$$

The energy distribution of ion fragments is related to delay time τ by:

$$C_{\text{Diss.}}(E,\tau) \propto \sum_{i} \left| \tilde{\Psi}_{\text{Diss.},i}(P,t) \right|^{2}, E = \frac{P^{2}}{2m}$$

▶ Fourier transforms of $C_{\text{Diss.}}$ give "beat frequencies" of KER

Previous CO⁺ experimental results



Features:

- ▶ Primary KER "streaks" between 0.4-0.6 eV and 0.6-0.8 eV, secondary streak between 0.2-0.4 eV
- ▶ Largest beat frequencies around 50 THz

 1 De S., et al., 2011

$X^2\Sigma^+$ coupled channel results



- Consistent with lower primary streak in experimental KER results
- ▶ No clear match in experimental power spectra

$A^2\Pi$ Results



- Consistent with lower primary streak in experimental KER results
- ▶ No clear match in experimental power spectra

$B^2\Sigma^+$ Results



- ▶ In same overall KER range as experimental results, but no clear match
- ▶ No clear match in experimental power spectra

Interpretation and future work

- Coupled channel simulations fail to explain experimental KER spectra
- No low-lying CO⁺ molecular potential curve explains 50 THz experimental power spectra results
- ► Future: more realistic simulations involving multi-coupled propagation between all low-lying potential curves
- ► Future: more realistic electronic transition models than Franck-Condon approximation
- ▶ Future: investigate laser-pulse dependence of KER

References

[1] De, S. et al. "Following dynamic nuclear wave packets in N_2 , O_2 , and CO with few-cycle infrared pulses." *Physical Review A* 84, 043410 (2011).

[2] Okada, K. and S. Iwata. "Accurate potential energy and transition dipole moment curves for several electronic states of CO⁺." J. Chem. Phys. 112.4 (2000): p.1804-1808.