

Prefixes

a=10⁻¹⁸, f=10⁻¹⁵, p=10⁻¹², n=10⁻⁹, μ = 10⁻⁶, m=10⁻³, c=10⁻², k=10³, M=10⁶, G=10⁹, T=10¹², P=10¹⁵

Physical Constants

$$k = 1/4\pi\epsilon_0 = 8.988 \text{ GNm}^2/\text{C}^2 \text{ (Coulomb's Law)}$$

$$e = 1.602 \times 10^{-19} \text{ C (proton charge)}$$

$$m_e = 9.11 \times 10^{-31} \text{ kg (electron mass)}$$

$$c = 3.00 \times 10^8 \text{ m/s (speed of light)}$$

$$\epsilon_0 = 1/4\pi k = 8.854 \text{ pF/m (permittivity of space)}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A (permeability of space)}$$

$$m_p = 1.67 \times 10^{-27} \text{ kg (proton mass)}$$

$$c = 2.99792458 \times 10^8 \text{ m/s (exact value in vacuum)}$$

Units

$$N_A = 6.02 \times 10^{23}/\text{mole (Avogadro's \#)}$$

$$1.0 \text{ eV} = 1.602 \times 10^{-19} \text{ J (electron-volt)}$$

$$1 \text{ F} = 1 \text{ C/V} = 1 \text{ farad} = 1 \text{ C}^2/\text{J}$$

$$1 \text{ A} = 1 \text{ C/s} = 1 \text{ ampere} = 1 \text{ coulomb/second}$$

$$1 \text{ T} = 1 \text{ N/A}\cdot\text{m} = 1 \text{ tesla} = 1 \text{ newton/ampere}\cdot\text{meter}$$

$$1 \text{ u} = 1 \text{ g}/N_A = 1.6605 \times 10^{-27} \text{ kg (mass unit)}$$

$$1 \text{ V} = 1 \text{ J/C} = 1 \text{ volt} = 1 \text{ joule/coulomb}$$

$$1 \text{ H} = 1 \text{ V}\cdot\text{s/A} = 1 \text{ henry} = 1 \text{ J/A}^2$$

$$1 \Omega = 1 \text{ V/A} = 1 \text{ ohm} = 1 \text{ J}\cdot\text{s/C}^2$$

$$1 \text{ G} = 10^{-4} \text{ T} = 1 \text{ gauss} = 10^{-4} \text{ tesla}$$

OpenStax Chapter 24 Equations - Electromagnetic Waves

Electromagnetic waves:

$$|\vec{E}|/|\vec{B}| = c = 1/\sqrt{\epsilon_0\mu_0}, \quad (\text{fields and speed})$$

$$\omega = 2\pi f = \frac{1}{\sqrt{LC}} \quad (\text{LC oscillator frequency})$$

$$f\lambda = c \quad (\text{wave equation})$$

$$x = ct \quad (\text{propagation in space})$$

Energy density, intensity, power:

$$u = \epsilon_0 E^2 = \frac{B^2}{\mu_0} \quad (\text{instantaneous energy density})$$

$$I = \bar{u}c = \frac{1}{2}\epsilon_0 E_0^2 c \quad (\text{EM waves intensity})$$

$$\bar{u} = \frac{1}{2}\epsilon_0 E_0^2 = \frac{B_0^2}{2\mu_0} \quad (\text{average energy density})$$

$$I = P/A = P/(4\pi r^2) \quad (\text{intensity definition})$$

Approximate wavelengths λ for types of EM waves:

0 (γ -rays) 30 pm (x -rays) 3 nm (uv) 400 nm (visible) 700 nm (ir) 300 μm (μ -waves) 3 cm (radio) ∞
→ → → increasing wavelength → → →

OpenStax Chapter 25 Equations - Geometrical Optics

Reflection, Mirrors:

$$\theta_r = \theta_i \quad (\text{angle of reflection} = \text{angle of incidence})$$

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \quad (\text{mirror equation})$$

$$d_i > 0 \Rightarrow \text{real, light side.}$$

$$m > 0 \Rightarrow \text{upright.}$$

$$|m| > 1 \Rightarrow \text{magnified.}$$

$$f = r/2 \quad (\text{focal length of spherical mirror})$$

$$m = -d_i/d_o = h_i/h_o \quad (\text{linear magnification})$$

$$d_i < 0 \Rightarrow \text{virtual, dark side.}$$

$$m < 0 \Rightarrow \text{inverted.}$$

$$|m| < 1 \Rightarrow \text{diminished.}$$

Refraction, Lenses:

$$n = c/v \quad (\text{index of refraction})$$

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \quad (\text{lens equation})$$

$$d_i > 0 \Rightarrow \text{real image, light (opp.) side.}$$

$$m > 0 \Rightarrow \text{upright.}$$

$$|m| > 1 \Rightarrow \text{magnified.}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2 \quad (\text{Snell's Law})$$

$$m = -d_i/d_o = h_i/h_o \quad (\text{linear magnification})$$

$$d_i < 0 \Rightarrow \text{virtual image, dark (same) side.}$$

$$m < 0 \Rightarrow \text{inverted.}$$

$$|m| < 1 \Rightarrow \text{diminished.}$$

Angles in radians

$$\theta = s/r \quad \text{angle} = \text{arc length} / \text{radius} = \text{separation} / \text{distance away.}$$

Lens power

$$P = 1/f \quad (\text{power in diopters, when } f \text{ is in meters}).$$

Cameras

$$f/D = \text{f-number, or lens aperture} \quad \text{film exposure} = \text{exposure time} / \text{f-number.}$$

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f} \quad (\text{lens equation}) \quad m = -d_i/d_o = h_i/h_o \quad (\text{linear magnification})$$

Vision correction

$$\text{Far point FP} = \infty. \quad (\text{good vision}) \quad \text{Near point} = \text{NP} \leq 25 \text{ cm. (good vision)}$$

$$\text{Nearsighted. Use lens to get FP}=\infty. \quad \text{Farsighted. Use lens to get NP}=25 \text{ cm.}$$

Simple magnifier

$$\theta = \frac{h_o}{\text{NP}} \quad (\text{angular size at NP, via bare eye}) \quad \theta' = \frac{h_o}{d_o} \quad (\text{angular size at } d_o, \text{ thru magnifier})$$

$$M = \frac{\theta'}{\theta} = \frac{\text{NP}}{d_o} \quad (\text{ang. Mag. viewed at any } d_o) \quad M = \frac{\theta'}{\theta} = \frac{\text{NP}}{f} \quad (\text{ang. Mag. viewed at } d_o = f)$$

Microscopes

$$\theta = \frac{h_o}{\text{NP}} \quad (\text{angular size of object at NP, via bare eye})$$

$$m_o = \frac{h_i}{h_o} = \frac{-d_i}{d_o} \quad (1^{\text{st}} \text{ image, linear magnification of objective lens})$$

$$M_e = \frac{\theta'}{\theta} = \frac{\text{NP}}{d'_o} \quad (\text{angular magnification due to eyepiece lens})$$

$$M = \frac{\theta_{\text{micro}}}{\theta} = m_o M_e \quad (\text{net angular magnification compared to bare eye})$$

Telescopes

$$M = \frac{\theta'}{\theta} = -\frac{f_{\text{obj}}}{f_{\text{eye}}} \quad (\text{angular magnification compared to bare eye})$$