

Prefixes

a=10⁻¹⁸, f=10⁻¹⁵, p=10⁻¹², n=10⁻⁹, μ = 10⁻⁶, m=10⁻³, c=10⁻², k=10³, M=10⁶, G=10⁹, T=10¹², P=10¹⁵

Physical Constants

$$k = 1/4\pi\epsilon_0 = 8.988 \text{ GNm}^2/\text{C}^2 \text{ (Coulomb's Law)}$$

$$e = 1.602 \times 10^{-19} \text{ C (proton charge)}$$

$$m_e = 9.11 \times 10^{-31} \text{ kg (electron mass)}$$

$$\epsilon_0 = 1/4\pi k = 8.854 \text{ pF/m (permittivity of space)}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A (permeability of space)}$$

$$m_p = 1.67 \times 10^{-27} \text{ kg (proton mass)}$$

Units

$$N_A = 6.02 \times 10^{23}/\text{mole (Avogadro's \#)}$$

$$1.0 \text{ eV} = 1.602 \times 10^{-19} \text{ J (electron-volt)}$$

$$1 \text{ F} = 1 \text{ C/V} = 1 \text{ farad} = 1 \text{ C}^2/\text{J}$$

$$1 \text{ A} = 1 \text{ C/s} = 1 \text{ ampere} = 1 \text{ coulomb/second}$$

$$1 \text{ T} = 1 \text{ N/A}\cdot\text{m} = 1 \text{ tesla} = 1 \text{ newton/ampere}\cdot\text{meter}$$

$$1 \text{ u} = 1 \text{ g}/N_A = 1.6605 \times 10^{-27} \text{ kg (mass unit)}$$

$$1 \text{ V} = 1 \text{ J/C} = 1 \text{ volt} = 1 \text{ joule/coulomb}$$

$$1 \text{ H} = 1 \text{ V}\cdot\text{s/A} = 1 \text{ henry} = 1 \text{ J/A}^2$$

$$1 \Omega = 1 \text{ V/A} = 1 \text{ ohm} = 1 \text{ J}\cdot\text{s/C}^2$$

$$1 \text{ G} = 10^{-4} \text{ T} = 1 \text{ gauss} = 10^{-4} \text{ tesla}$$

OpenStax Chapter 18 Equations

Charges:

$$Q = \pm Ne, \quad \Delta Q_1 + \Delta Q_2 = 0, \quad e = 1.602 \times 10^{-19} \text{ C.}$$

Electric Force:

$$F = k \frac{Q_1 Q_2}{r^2}, \quad k = 8.988 \times 10^9 \text{ N}\cdot\text{m}^2/\text{C}^2,$$

$$F = \frac{Q_1 Q_2}{4\pi\epsilon_0 r^2}, \quad \epsilon_0 = \frac{1}{4\pi k} = 8.854 \text{ pF/m.}$$

$$\vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots \quad \text{superposition of forces.}$$

Electric Field:

$$\vec{E} = \frac{\vec{F}}{q}, \quad q = \text{test charge.} \quad \text{Or: } \vec{F} = q\vec{E}.$$

$$|\vec{E}| = E = k \frac{Q}{r^2} = \frac{Q}{4\pi\epsilon_0 r^2}, \quad \text{due to point charge. Negative } Q \text{ makes inward } \vec{E}, \text{ positive } Q \text{ makes outward } \vec{E}.$$

$$\vec{E} = \vec{E}_1 + \vec{E}_2 + \vec{E}_3 + \dots \quad \text{superposition of many electric fields.}$$

$$E = k \frac{Q}{r^2} = \text{electric field around a point charge or } \textit{outside} \text{ a spherical charge distribution.}$$

OpenStax Chapter 19 Equations

Potential Energy and Work:

$$W_{ba} = F_E d \cos \theta = \text{work done by electric force } F_E \text{ on test charge, in displacement } d \text{ from } a \text{ to } b.$$

$$W_{ba} = -q\Delta V = -q(V_b - V_a) = \text{work done by electric force on a test charge, moved from } a \text{ to } b.$$

$$\Delta \text{PE} = q\Delta V = q(V_b - V_a) = \text{change in electric potential energy of the system. Also: } \Delta \text{PE} = -W_{ba}.$$

Potential:

$$\Delta V = \frac{\Delta \text{PE}}{q} = \text{definition of change in electric potential.}$$

$$\Delta V = Ed = \text{potential change in a uniform electric field.}$$

$$V = k \frac{Q}{r} = \text{potential produced by a point charge or } \textit{outside} \text{ a spherical charge distribution.}$$

$$\text{PE} = qV = \text{potential energy for a test charge at a point in a field.}$$

$$\text{PE} = k \frac{Q_1 Q_2}{r_{12}} = \text{potential energy of a pair of charges.}$$

Capacitance:

$$Q = CV, \quad C = K\epsilon_0 \frac{A}{d} = \text{capacitor equations.}$$

$$U = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2} \frac{Q^2}{C} = \text{stored energy.}$$

$$E = \frac{Q/A}{\epsilon_0} = \text{electric field strength very near a charged conductor.}$$

OpenStax Chapter 20 Equations

Electric current and power:

$$I = \frac{\Delta Q}{\Delta t}, \quad \Delta Q = I\Delta t \quad \text{current definition.}$$

$$R = \rho L/A \quad \text{calculation of resistance.}$$

$$P = IV, \quad P = I^2R, \quad P = V^2/R.$$

$$V = IR, \quad I = V/R \quad \text{Ohm's law.}$$

$$\rho = \rho_0[1 + \alpha(T - T_0)] \quad \text{resistivity changes.}$$

$$P = \text{instantaneous work/time.}$$

Alternating current:

$$V = V_0 \sin(2\pi ft) = \text{time-dependent AC voltage.}$$

$$I = I_0 \sin(2\pi ft) = \text{time-dependent AC current.}$$

$$V_{\text{rms}} = \sqrt{\overline{V^2}} = V_0/\sqrt{2} = \text{root-mean-square voltage.}$$

$$I_{\text{rms}} = \sqrt{\overline{I^2}} = I_0/\sqrt{2} = \text{root-mean-square current.}$$

AC power:

$$\overline{P} = \frac{1}{2}I_0V_0 = \frac{1}{2}I_0^2R = \frac{1}{2}V_0^2/R = \text{average power.}$$

$$\overline{P} = I_{\text{rms}}V_{\text{rms}} = I_{\text{rms}}^2R = V_{\text{rms}}^2/R = \text{average power.}$$

OpenStax Chapter 21 Equations

Resistor Combinations

$$R_{\text{eq}} = R_1 + R_2 + R_3 + \dots \quad (\text{series})$$

$$\frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} + \dots \quad (\text{parallel})$$

Real batteries

$$V_{ab} = \mathcal{E} - Ir \quad (\text{terminal voltage})$$

$$V_{ab} = IR \quad (\text{connected to load } R)$$

Kirchhoff's Rules

$$\sum \Delta V = 0 \quad (\text{loop rule, energy conservation})$$

$$\sum I = 0 \quad (\text{node rule, charge conservation})$$

OpenStax Chapter 22 Equations

Magnetic forces, torque

$$F = I\ell B \sin \theta \quad (\text{on a current})$$

$$F = qvB \sin \theta \quad (\text{on a moving charge})$$

$$F/l = \frac{\mu_0}{2\pi} \frac{I_1 I_2}{d} \quad (\text{between currents})$$

$$F = qvB = mv^2/r \quad (\text{during cyclotron motion})$$

$$\tau = NBAI \sin \theta \quad (\text{torque on a coil})$$

$$v = \omega r = 2\pi fr = 2\pi r/T \quad (\text{circular motion})$$

Magnetic Fields

$$B = \frac{\mu_0}{2\pi} \frac{I}{r} \quad (\text{due to long straight wire})$$

$$B = \mu_0 IN/l \quad (\text{inside a solenoid})$$

Right Hand Rules

$$\text{Force (thumb)} = [I \text{ (4 fingers)}] \times [\text{magnetic field (palm)}] \quad (\text{force on a current})$$

$$\text{Force (thumb)} = [qv \text{ (4 fingers)}] \times [\text{magnetic field (palm)}] \quad (\text{force on a moving charge})$$

$$\text{Current (thumb)} \iff [\text{magnetic field (4 fingers)}] \quad (\text{magnetic field around a wire})$$

$$\text{Current (4 fingers)} \iff [\text{magnetic field (thumb)}] \quad (\text{magnetic field inside a current loop})$$

OpenStax Chapter 23 Equations

Faraday's Induced EMF

$$\Phi_B = BA \cos \theta \quad (\text{magnetic flux})$$

$$\mathcal{E} = -N \frac{\Delta \Phi_B}{\Delta t} \quad (\text{induced emf})$$

$$\mathcal{E} = Blv \quad (\text{moving conductor})$$

$$\mathcal{E} = NBA\omega \sin(\omega t), \quad \omega = 2\pi f \quad (\text{AC generator})$$

$$V - \mathcal{E} = IR \quad (\text{motor's back-emf})$$

$$\mathcal{E}_1 = -M \frac{\Delta I_2}{\Delta t} \quad (\text{mutual inductance emf})$$

$$V_S/V_P = N_S/N_P \quad (\text{transformer equation})$$

$$I_P V_P = I_S V_S \quad (\text{power in} = \text{power out})$$

AC Circuits, Inductors, Capacitors, Reactance

$$\mathcal{E} = -L \frac{\Delta I}{\Delta t} \quad (\text{self-inductance emf})$$

$$U = \frac{1}{2} LI^2 \quad (\text{stored magnetic energy})$$

$$X_L = 2\pi fL = \omega L \quad (\text{inductive reactance})$$

$$V_L = IX_L \quad (\text{inductor voltage})$$

$$X_C = 1/(2\pi fC) = 1/(\omega C) \quad (\text{capacitive reactance})$$

$$V_C = IX_C \quad (\text{capacitor voltage})$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2} \quad (\text{series RLC impedance})$$

$$V_{\text{gen}} = IZ = \sqrt{V_R^2 + (V_L - V_C)^2} \quad (\text{series RLC})$$

$$\omega_0 = 1/\sqrt{LC}, \quad f_0 = \frac{\omega_0}{2\pi} \quad (\text{LC resonance})$$

$$\tan \phi = (X_L - X_C)/R \quad (\text{series RLC phase})$$

$$\overline{P} = I_{\text{rms}} V_{\text{rms}} \cos \phi \quad (\text{AC average power})$$

$$\overline{P} = I_{\text{rms}}^2 R \quad (\text{series RLC})$$