

Prefixes

a=10⁻¹⁸, f=10⁻¹⁵, p=10⁻¹², n=10⁻⁹, μ = 10⁻⁶, m=10⁻³, c=10⁻², k=10³, M=10⁶, G=10⁹, T=10¹², P=10¹⁵

Physical Constants

$g = 9.80 \text{ m/s}^2$ (gravitational acceleration)
 $M_E = 5.98 \times 10^{24} \text{ kg}$ (mass of Earth)
 $m_e = 9.11 \times 10^{-31} \text{ kg}$ (electron mass)
 $c = 299792458 \text{ m/s}$ (speed of light)

$G = 6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2$ (Gravitational constant)
 $R_E = 6380 \text{ km}$ (mean radius of Earth)
 $m_p = 1.67 \times 10^{-27} \text{ kg}$ (proton mass)

Units and Conversions

1 inch = 1 in = 2.54 cm (exactly)
1 mile = 5280 ft
1 m/s = 3.6 km/hour
1 acre = 43560 ft² = (1 mile)²/640

1 foot = 1 ft = 12 in = 30.48 cm (exactly)
1 mile = 1609.344 m = 1.609344 km
1 ft/s = 0.6818 mile/hour
1 hectare = 10⁴ m²

Chapter 1 Equations

Percent error:

If a measurement = value \pm error, the percent error = $\frac{\text{error}}{\text{value}} \times 100 \%$.

Chapter 2 Equations

Motion:

$$\bar{v} = \frac{\Delta x}{\Delta t}, \quad \Delta x = x - x_0, \quad \text{slope of } x(t) \text{ curve} = v(t).$$
$$\bar{a} = \frac{\Delta v}{\Delta t}, \quad \Delta v = v - v_0, \quad \text{slope of } v(t) \text{ curve} = a(t).$$

For constant acceleration in one-dimension:

$$\bar{v} = \frac{1}{2}(v_0 + v), \quad v = v_0 + at, \quad x = x_0 + v_0t + \frac{1}{2}at^2, \quad v^2 = v_0^2 + 2a(x - x_0).$$

For free fall on Earth, using an upward y -axis, with $g = 9.80 \text{ m/s}^2$ downward:

$$\bar{v}_y = \frac{1}{2}(v_{y0} + v_y), \quad v_y = v_{y0} - gt, \quad y = y_0 + v_{y0}t - \frac{1}{2}gt^2, \quad v_y^2 = v_{y0}^2 - 2g\Delta y.$$

Chapter 3 Equations

Vectors

Written \vec{V} or \mathbf{V} , described by magnitude= V , direction= θ or by components (V_x, V_y).

$$V_x = V \cos \theta, \quad V_y = V \sin \theta,$$

$$V = \sqrt{V_x^2 + V_y^2}, \quad \tan \theta = \frac{V_y}{V_x}. \quad \theta \text{ is the angle from } \vec{V} \text{ to } x\text{-axis.}$$

Addition: $\mathbf{A} + \mathbf{B}$, head to tail. Subtraction: $\mathbf{A} - \mathbf{B}$ is $\mathbf{A} + (-\mathbf{B})$, $-\mathbf{B}$ is \mathbf{B} reversed.

Projectiles

$$a_x = 0, \quad v_x = v_{x0}, \quad x = x_0 + v_{x0}t. \quad \text{For a horizontal } x\text{-axis.}$$

$$a_y = -g, \quad v_y = v_{y0} - gt, \quad y = y_0 + v_{y0}t - \frac{1}{2}gt^2. \quad \text{For an upward } y\text{-axis.}$$

$$R = \frac{v_0^2}{g} \sin 2\theta_0, \quad (\text{For level ground only.})$$

Relative Motion

$$\vec{V}_{BS} = \vec{V}_{BW} + \vec{V}_{WS},$$

B=Boat, S=Shore, W=Water.

BS means "boat relative to shore", etc.

Must be applied as a vector equation!

Trig summary

$$\sin \theta = \frac{(\text{opp})}{(\text{hyp})}, \quad \cos \theta = \frac{(\text{adj})}{(\text{hyp})}, \quad \tan \theta = \frac{(\text{opp})}{(\text{adj})}, \quad (\text{opp})^2 + (\text{adj})^2 = (\text{hyp})^2.$$

$$\sin \theta = \sin(180^\circ - \theta), \quad \cos \theta = \cos(-\theta), \quad \tan \theta = \tan(180^\circ + \theta), \quad \sin^2 \theta + \cos^2 \theta = 1.$$