Dissociation dynamics of diatomic molecules in intense laser fields: A scheme for the selection of relevant adiabatic potential curves

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We investigated the nuclear dynamics of diatomic molecular ions in intense laser fields by analyzing their fragment kinetic-energy release (KER) spectra as a function of the pump-probe delay \( \tau \). Within the Born-Oppenheimer (BO) approximation, we calculated \textit{ab initio} adiabatic potential-energy curves and their electric dipole couplings, using the quantum chemistry code GAMESS. By comparing simulated KER spectra as a function of either \( \tau \) or the vibrational quantum-beat frequency for the nuclear dynamics on both individual and dipole-coupled BO potential curves with measured spectra, we developed a scheme for identifying electronic states that are relevant for the dissociation dynamics. We applied this scheme to investigate the nuclear dynamics in \( \text{O}_2^+ \) ions that are produced by ionization of neutral \( \text{O}_2 \) molecules in an ultrashort infrared (IR) pump pulse and dissociate due to the dipole coupling of molecular potential curves in a delayed IR probe laser field.

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I. INTRODUCTION

The control, time-resolved observation, and analysis of the nuclear dynamics in small diatomic molecules have been made possible by significant advances in femtosecond laser technology [1,2]. In particular, using ultrashort IR pulses with a carrier wavelength of 800 nm and pulse lengths between 7 and 20 fs, the nuclear dynamics in \( \text{H}_2 \) and \( \text{D}_2 \) molecular ions have been studied by analyzing the kinetic-energy release (KER) of the fragments produced by a second delayed laser pulse [3,4]. In comparison with heavier molecules, the vibrational nuclear motion in \( \text{H}_2^+ \) (and its isotopes) is simple as it primarily involves the two lowest adiabatic potential curves of the molecular ion. For \( \text{H}_2^+ \), the dissociative wave packet emerges mainly on the repulsive \( |2p\sigma_u\rangle \) state, while a bound oscillating part of the wave packet may remain in the electronic ground state \( |1s\sigma_g\rangle \). The extension of these investigations to heavier molecules is not straightforward, and the interpretation of experimental data is intricate due to the large number of molecular potential curves involved. By analyzing KER spectra from dissociated oxygen ions as a function of the time delay, we recently found that usually several intermediate electronic states of the molecular ion contribute to the same KER [5–7]. In Refs. [5,7] the dynamics of \( \text{N}_2 \), \( \text{O}_2 \), and \( \text{CO} \) molecules in intense laser pulses was studied using the Coulomb explosion (CE) imaging technique. In comparison with classical and quantum-mechanical simulations, transiently populated intermediate states for molecular ions in different charge states and associated dissociation pathways were identified. The occurrence of vibrational revivals in measured KER spectra was scrutinized in Ref. [6] and allowed the identification of relevant molecular potential curves.

The purpose of this work is to systematically combine and jointly evaluate the information contained in different characteristic signatures of measured KER spectra. By revealing different aspects of the oscillating and dissociating motion in heavy diatomic molecular ions, we attempt to identify a manageable number of \textit{relevant} electronic states within a large set of possible BO electronic states that exist for each heavy diatomic molecule in each charge state. We start our investigation in Sec. II by employing the General Atomic and Molecular Electronic Structure System (GAMESS) quantum chemistry code [8] to calculate potential curves and dipole coupling strengths between adiabatic potential curves using the multiconfiguration (MC) self-consistent field (SCF) method with correlation consistent (cc) polarized triple-\( \zeta \) (pVTZ) basis sets (MCSCF cc-pVTZ) [9,10].

Next, in Sec. IIIA, we numerically solve the time-dependent Schrödinger equation (TDSE) for the evolution of a given initial vibrational wave packet in the molecular ion on a given BO potential curve. In our quantum-mechanical calculations, we neglect molecular rotation and model the initial state of the molecular ion by assuming instantaneous ionization of the neutral parent molecule in the pump pulse based on the Franck-Condon approximation [11]. Our calculations provide KER spectra as a function of the pump-probe delay that reveal the vibrational period and revival times of binding molecular potential curves. The vibrational period and revival times in a \textit{given} electronic state serve as a first criterion for selecting relevant potential curves. This selection process starts by comparing simulated KER spectra that were obtained in separate calculations under the assumption that the nuclear motion in the molecular ion proceeds on a single electronic potential curve with measured KER spectra. This comparison involves the scrutiny of simulated and measured KER spectra as a function of time and frequency. For this purpose we derive internuclear-distance-dependent power spectra [12–14] by Fourier transformation of the calculated time-dependent nuclear probability density. The power spectra allow us to identify vibrational quantum-beat (QB) frequencies associated with the bound motion of the vibrationally excited molecular ion. This enables us to further scrutinize the relevance of any given binding electronic state of the molecular ion by comparing revival times [15], oscillation periods, and QB frequencies with measured values.

After comparing separate calculations performed for individual BO molecular potential curves with measured KER spectra, we select a small set (in this work two) of curves
that agree best with the measured data. In a final separate calculation, we then investigate the dissociative dynamics of the molecule, including dipole couplings between the selected electronic states of the molecular ion in the electric field of the probe-laser pulse (Sec. III B). As an example we present numerical results for the dissociation of $O_2^{+}$ molecules. In Sec. III C we compare two alternative methods for deriving KER spectra in a nuclear wave-function-propagation calculation. The effect of an added long probe pedestal is investigated in Sec. III D. Section IV compares measured KER spectra for $O_2^{+}$ ions with simulated spectra for dipole-coupled potential curves. A brief summary and our conclusions follow in Sec. V.

II. CALCULATION OF ADIABATIC POTENTIAL CURVES

To describe molecules in an intense laser field accurately one needs to consider both the electronic and nuclear degrees of freedom. The Hamilton operator for the unperturbed diatomic molecular system includes the kinetic energies of the nuclei and electrons $T_R$ and $T_e$, the interaction between the nuclei $V_{RR} = Z_1 Z_2 / R$, and the electrons $V_{ee} = \sum_{i<j} r_{ij}^{-1}$, and the electron-nuclear interaction $V_{eR} = \sum_{i} \sum_{k} Z_k r_{ik}^{-1}$.

$$H = T_R + V_{RR} + T_e + V_{eR} + V_{ee}.$$  \hspace{1cm} (1)

$Z_1$ and $Z_2$ are the nuclear charges, $R$ is internuclear distance, $r_{ij}$ is the distance between two electrons with labels $i$ and $j$, and $r_{ik}$ is the distance between the nuclei and electrons labeled $k$ and $i$, respectively.

No exact solutions of the Schrödinger equation with Hamiltonian (1) are known. However, a simplified solution can be obtained within the BO approximation where the total wave function (WF) is expanded in products of nuclear and electronic WFs. The BO approximation is based on the fact that electrons are several thousand times lighter than nuclei and thus can be assumed to follow the nuclear motion adiabatically. This means that the nuclear kinetic energy term $T_R$ in Eq. (1) can be dropped and that $V_{RR}$ becomes a constant and thus is irrelevant for the electronic motion considered in this work. In BO approximation accurately evaluating the correlation between electrons $V_{ee}$ remains a challenge for numerical calculations. To overcome this difficulty, the so-called Hartree-Fock (HF) SCF method is used [16,17] in order to include the effect of $V_{ee}$ approximately by considering each electron subject to an effective potential that is derived from the averaged charge distribution of all other electrons.

We used the MCSCF method, where a linear combination of configuration state functions (CSF), i.e., Slater determinants of molecular orbitals (MO), is employed to approximate the exact electronic WF of the system. This is an improvement over the HF method, where only one determinant is used. By variation of the set of coefficients in the MCSCF expansion in addition to the simultaneous variation of MO coefficients in the basis-set expansion, the total electronic WF for a given BO channel is obtained with the lowest possible energy for a given set of occupied and active orbitals [16,17]. We calculated potential curves and dipole-coupling strengths between adiabatic potential curves using the MCSCF–cc-pVTZ method (details are given in the Appendix).

A. Results

Figure 1 shows some of the calculated electronic states for the $O_2^{+}$ molecular ion. For selected states we compared data from the literature [18] with our MCSCF–cc-pVTZ results and found good agreement for both adiabatic potential curves and electric dipole transition matrix elements $D_{ij}$ between adiabatic electronic states that correspond to potential curves $V_i(R)$ and $V_j(R)$. As an example, our calculated potential curves and dipole-coupling matrix elements for the $a^4\Pi_u$ and $f^4\Pi_g$ states of $O_2^{+}$ are compared to results in Ref. [18] in Figs. 2(a) and 2(b), respectively. In Marian et al. [18], multireference double-excitation configuration interaction (MRD-CI) treatment [19] and a double-$\zeta$ basis set were used in the calculation (MRD-CI DZP). MRD-CI includes electron correlation from excited determinants in addition to correlation within the active space.

To make sure that our MCSCF–cc-pVTZ method was sufficient compared to calculations that better represent electron correlation, we performed full second-order CI calculations (FSOCI) for the $a^4\Pi_u$ state at four different internuclear distances. FSOCI calculations are similar to MRD-CI but include single and double excitations, while MRD-CI includes only double excitations. Blue dots in Fig. 2(a) indicate results from FSOCI–cc-pVTZ calculations, which are in good agreement (within 0.7%) with our MCSCF calculations [red (gray) line in Fig. 2(a)]. The computational time for FSOCI calculations is three orders of magnitude larger than for MCSCF calculations. Since the calculated values from both methods are similar, we used the numerically less expensive method (MCSCF) to obtain electronic states and dipole-coupling matrix elements. Using a larger cc-pVTZ basis set than the basis used in Ref. [18], we can be confident that our calculated results are at least as accurate with regard to the complete basis set limit.
Fig. 2. (Color online) (a) Calculated potential energies and (b) dipole-coupling matrix elements from [18] using the MRD-CI-DZD method in comparison with our MCSCF-cc-pVTZ calculation. Blue dots in (a) correspond to the FSOCI-cc-pVTZ method.

FIG. 3. (Color online) The nuclear dynamics in oxygen molecular ions. The pump-laser pulse launches a nuclear vibrational wave packet onto $O_2^+$ potential curves (shown for $a \Pi_u$ and $f \Pi_u$ states) by ionizing $O_2$. After a variable time delay, an intense short probe pulse can cause the dissociation of the molecular ion through one-photon or net two-photon processes.

III. NUCLEAR DYNAMICS

A. Free nuclear motion in a single electronic state

The dynamics of the nuclear vibrational wave packet can be reconstructed from the KER spectra obtained for a sequence of pump-probe delays $T$. This is shown schematically in Fig. 3 for the $a \Pi_u$ and $f \Pi_u$ states where a pump pulse singly ionizes an oxygen molecule. In general, the pump pulse can ionize oxygen molecules to any state of $O_2^+$, for example, $X^2 \Pi_g$ and $b^4 \Sigma_g^-$ states, but as our calculations show, several characteristic parameters, such as oscillation period, revival time, and QB frequency for the $a \Pi_u$ state, match the experimental data best. The probe pulse is assumed to be linearly polarized along the molecular axis throughout this work. The excited oxygen molecule can dissociate through a one-photon or net two-photon process.

In order to reveal relevant intermediate electronic states of the molecular ion, we compared oscillation period and revival times of the bound motion of the wave packet in a given electronic state with measured values. We also checked whether transitions between these states are dipole allowed and calculated the strength of their dipole coupling in the electric field.

To identify which of the states are main contributors in the dynamics, we allowed the wave packet to freely propagate on individual adiabatic potential curves $V_i(R)$ of the molecular ion. Neglecting molecular rotation, we solved the one-dimensional TDSE,

$$i \frac{\partial}{\partial t} \Psi_i = [T_R + V_i(R)] \Psi_i,$$

where the $V_i$ are adiabatic potential curves.

Starting with neutral $O_2$ molecules in the ground state, we modeled the creation of the $O_2^+$ vibrational wave packet by the pump pulse in Frank-Condon approximation [11,12]. We solved (2) for the initial wave packet,

$$\Psi_i(R, t = 0) = \sum_{j} a_{i,j} \phi_{i,j}(R),$$

which is expressed in terms of the Franck-Condon amplitudes $a_{i,j}$. The indices $j$ correspond to vibrational states $\phi_{i,j}$ in the $i$th bonding adiabatic electronic state of the molecular ion with vibrational energy $\omega_{i,j}$.

By either calculating the spectrum $\omega_{i,j}$ by diagonalization of the single-curve Hamiltonian $T_R + V_i(R)$ or by numerical wave-packet propagation of (2) subject to the initial condition (3), we obtained the evolution of (3) without external laser fields,

$$\Psi_i(R, t) = \sum_{j} a_{i,j} \phi_{i,j}(R) e^{-i\omega_{i,j} t}.$$ 

Repeating single-curve calculations for several potential-energy curves, we aimed at identifying relevant electronic states by comparing the characteristics of the bound wave-packet motion in $V_i(R)$, such as vibrational periods $T_i$ and full and partial revival times $T_{rev,i}$ [15], that we obtained from probability density spectra [Figs. 4(a) and 4(c)], with pump-probe-delay-dependent measured KER data [5–7,12–14,20,21].

We obtained additional information for selecting electronic states that participate in the bound and dissociative nuclear motion of the molecular ion by comparing probability densities obtained from single-curve calculations with measured KER spectra as a function of the pump-probe delay (propagation time) and QB frequency [12–14]. By splitting the nuclear
A power spectra of the evolving vibrational wave packet and (b), (d) corresponding adiabatic electronic states of O$_2$.

FIG. 4. (Color online) Single-curve calculations for the (a), (b) $A \ ^{3}\Pi_{u}$ and (c), (d) $a \ ^{4}\Pi_{u}$ states of O$_2$.$^+$. (a), (c) Probability densities of the evolving vibrational wave packet and (b), (d) corresponding power spectra.

Probability density

$$\rho_i(R,t) = |\Psi_i(R,t)|^2 = \rho_i^{\text{incoh}}(R) + \sum_{\nu \neq \mu} a_{i,\nu}^{*} a_{i,\mu} \exp(-i \omega_{\nu,\mu} t) \phi_{i,\nu}^{*} \phi_{i,\mu} \quad \text{(5)}$$

into the time-independent incoherent contribution

$$\rho_i^{\text{incoh}}(R,t) = \sum_{\nu} |a_{i,\nu}|^2 |\phi_{i,\nu}(R)|^2 \quad \text{(6)}$$

and the time-dependent coherent contribution

$$\rho_i(R,\omega; T) = \frac{1}{\sqrt{\pi}} \int_0^T dt [\rho_i(R,t) - \rho_i^{\text{incoh}}(R)] e^{-i\omega t}$$

$$= \sqrt{2\pi} \sum_{\nu \neq \mu} a_{i,\nu}^{*} a_{i,\mu} \phi_{i,\nu}^{*}(R) \phi_{i,\mu}(R) \delta(T(\omega_{\nu,\mu} - \omega)) \quad \text{(7)}$$

and the power spectrum

$$W_i(R,\omega) = |\tilde{\rho}(R,\omega; T)|^2,$$ (8)

where $\delta_T(\Omega) = 1/2\pi \int_0^T e^{i\Omega t} dt$. The frequency resolution in $W_i$ increases with the sampling time $T$. Typically, sampling times of the order of a few picoseconds are required to clearly resolve vibrational beat frequencies in the power spectrum of heavy diatomic molecular ions.

Examples for single-curve calculations are shown in Figs. 4(a) and 4(b) for the $A \ ^{3}\Pi_{u}$ state and in Figs. 4(c) and 4(d) for the $a \ ^{4}\Pi_{u}$ state of O$_2$.$^+$. The calculations were done with a numerical grid length of 310 (excluding the absorber length of 20) and a grid spacing 0.05 with time steps of $\Delta t = 1$. We also performed the same calculations for $X \ ^{3}\Pi_{g}$ and $b \ ^{3}\Sigma_{g}^-$ states of O$_2$.$^+$ (Fig. 3, not shown in Fig. 4). Comparison of the simulated vibrational periods, revival times, and QB frequencies for a number of electronic states with measured KER spectra [7] revealed the $a \ ^{4}\Pi_{u}$ state as the best match to the experimental oscillation period and QB frequencies. Table I shows a comparison of the calculated and measured parameters for each potential curve we tried in our calculations. Table I reveals that closest to the experimental revival time of 1200 fs are the $A \ ^{3}\Pi_{u}$ and $A \ ^{4}\Pi_{u}$ states. However, the $A \ ^{3}\Pi_{u}$ state can be ruled out because it generates QB frequencies that do not match the measured frequencies. Thus, state $a \ ^{4}\Pi_{u}$ appears to be the most relevant in the dissociative dynamics, which is also in agreement with the experimental findings in Refs. [7,20].

Table I. Comparison of calculated (this work) and measured (Ref. [7]) revival times and ($\nu = 1 \rightarrow \nu = 2$) QB frequencies for four adiabatic electronic states of O$_2$.$^+$

<table>
<thead>
<tr>
<th>State</th>
<th>Oscillation period (fs)</th>
<th>Revival (fs)</th>
<th>QB frequency (THz)</th>
<th>Experimental values</th>
</tr>
</thead>
<tbody>
<tr>
<td>$X \ ^{3}\Pi_{g}$</td>
<td>17</td>
<td>670</td>
<td>58</td>
<td>34</td>
</tr>
<tr>
<td>$a \ ^{4}\Pi_{u}$</td>
<td>33</td>
<td>1000</td>
<td>30</td>
<td>$\sim 1200$</td>
</tr>
<tr>
<td>$A \ ^{3}\Pi_{u}$</td>
<td>36</td>
<td>1100</td>
<td>28</td>
<td></td>
</tr>
<tr>
<td>$b \ ^{3}\Sigma_{g}^-$</td>
<td>29</td>
<td>900</td>
<td>35</td>
<td></td>
</tr>
</tbody>
</table>

B. Nuclear dynamics on dipole-coupled electronic states

Modeling the coherent motion of nuclear vibrational wave packets on several Franck-Condon-populated adiabatic potential curves of the diatomic molecular ion, we allowed for dipole coupling of (coherently launched) nuclear wave packets $\Psi_i(R,t)$ in the electric field of the probe laser pulse by numerically propagating the coupled TDSE,

$$i \frac{\partial}{\partial t} \begin{pmatrix} \Psi_1 \\ \Psi_2 \\ \vdots \end{pmatrix} = \begin{pmatrix} T_R + V_1 & D_{12} & \cdots \\ D_{21} & T_R + V_2 & \cdots \\ \vdots & \cdots & \ddots \end{pmatrix} \begin{pmatrix} \Psi_1 \\ \Psi_2 \\ \vdots \end{pmatrix}, \quad \text{(9)}$$

using the split-operator Crank-Nicolson scheme, with the assumption that the wave packet is launched from the ground state of O$_2$ to the $V_1$ state of O$_2$.$^+$ [12–14]. In analogy to (4)–(7), Fourier transformation of the total nuclear probability density,

$$\rho(R,t) = \sum_i \rho_i(R,t), \quad \text{(10)}$$
for a finite sampling time $T$ results in

$$\bar{\rho}(R,\omega; T) \sim \sum_i \rho_i(R,\omega; T)$$

$$\sim \sum_i \sum_{\mu \neq \nu} \alpha_i^\mu \alpha_i^{\mu*} \phi_i^{\mu*}(R)\phi_i^{\mu}(R) \delta_T(\omega_{\mu,v} - \omega)$$

(11)

and the power spectrum

$$W(R,\omega) = |\bar{\rho}(R,\omega; T)|^2.$$  (12)

In order to simulate KER spectra, we numerically propagated the coupled equations (9) for a sufficiently long time, including field-free propagation of the nuclear wave packets up to $\sim 800$ fs after the Gaussian-shaped 10-fs-long probe pulse. This allowed us to separate the bound and dissociating parts of the nuclear motion by introducing the internuclear distance $R$ as an effective range for the bound nuclear motion. $R_1$ was determined such that the probability current associated with the dissociation of the molecular ion has relevant contributions only for $R > R_1$, whereas bound motion remained restricted to distances $R < R_1$ (Fig. 5). Fourier transformation of the dissociating parts of the nuclear wave packets over the interval $[R_1, R_{\text{max}}]$ yields the momentum representations of the dissociating wave packets in the adiabatic channel $i$,

$$\tilde{\Psi}_i^{\text{diss}}(P,T) = \int_{R_1}^{R_{\text{max}}} dR \, \Psi_i^{\text{diss}}(R,T) e^{-iPR},$$

(13)

where $R_{\text{max}}$ is related to the size of the numerical grid and $R_1$ is of the order of 4 in our applications below. By incoherently adding the corresponding momentum distributions $ho^{\text{incob}}(P,T) = |\tilde{\Psi}_i^{\text{diss}}(P,T)|^2$, we obtained the pump-probe-delay-dependent distribution of fragment KERs,

$$C^{\text{diss}}(E,\tau) \propto \sum_i \rho_i^{\text{incob}}(P,\tau),$$

(14)

where $E = P^2/2M$ is the kinetic energy per fragment, with $M$ being the nuclear mass. Subtracting the large incoherent static contribution

$$C^{\text{diss}}_{\text{incob}}(E) = \frac{1}{T} \int_0^T d\tau \, C^{\text{diss}}(E,\tau)$$

(15)

from $C^{\text{diss}}$, we obtained the power spectrum as a function of the beat frequency $f = \omega/2\pi$,

$$p^{\text{diss}}(E,f) = \left| \int_0^T d\tau \, C^{\text{diss}}_{\text{coh}}(E,\tau) e^{-i2\pi f\tau} \right|^2.$$  (16)

We refer to this method as the “Fourier-transformation (FT)” method.

After conducting single-curve calculations for several potential curves of O$_2$ and identifying adiabatic electronic states, we solved the TDSE for the dipole-coupled $a^4\Pi_u$ and $f^4\Pi_u$, $a^4\Pi_u$ and $4\Sigma^+_g$, and $A^4\Pi_u$ and $2\Sigma^+_g$ states in order to investigate the dissociation channels involved. The best match to the measured KER was obtained with the $a^4\Pi_u$-$f^4\Pi_g$ two-state calculation.

Figure 5(a) shows the probability density [see Eqs. (5) or (10)] as a function of propagation time and internuclear distance at a fixed pump-probe delay ($\tau = 10$ fs) for a calculation with two coupled states, $a^4\Pi_u$ and $f^4\Pi_g$. In this calculation we assumed that, initially, only the $a^4\Pi_u$ state is populated, through a Franck-Condon transition from the ground state of O$_2$. Physically, this assumption can be justified by the fact that molecular ionization rates tend to be largest for states of the molecular ion that are energetically closest to the ground state of the neutral molecule. In our case this favors the initial population of the $X^2\Pi_g$ ground state of O$_2$. However, we also found that (i) the vibrational period in the $X^2\Pi_g$ state is not at all seen in the experimental spectra and (ii) due to the strongly binding nature of this state, it does not contribute to dissociation (for the range of laser parameters we considered). In contrast, the next higher-lying bonding $a^4\Pi_u$ state of the molecular ion is shallow enough to strongly contribute to dissociation and therefore is assumed to be the (by far) most relevant populated initial state. Also, we found that the KER spectra do not change if initially both $a^4\Pi_u$ and $f^4\Pi_g$ states are equally populated. The delayed probe pulse couples the initial wave packet motion with the $f^4\Pi_g$ state. As mentioned above, for the KER spectra calculations we took only the dissociative part of the wave packet into account. The horizontal yellow dashed line indicates the internuclear separation $R_1 = 4$, beyond which the wave packet is considered as purely dissociative. Figure 5(b) shows the probability density on a logarithmic scale as a function of the internuclear distance 800 fs after the pump pulse.

We investigated the effect of parameter $R_1$ on the KER spectra. The calculated KER, obtained using the FT method, as a function of pump-probe delay is given in Fig. 6 for 10 fs, $3 \times 10^{14}$ W/cm$^2$ probe pulses and for $R_1 = 3$ [Fig. 6(a)], $R_1 = 4$ [Fig. 6(b)], $R_1 = 4.5$ [Fig. 6(c)], and $R_1 = 5$ [Fig. 6(d)]. From Fig. 5(b) one can see that for all values $R_1 > 4.5$ the KER spectra should give the same result. Indeed, the KER spectra shown in Figs. 6(c) ($R_1 = 4.5$) and 6(d) ($R_1 = 5$) are almost the same. We found that simulations with $R_1 = 4$ yield the best agreement with measured KER spectra (see Sec. IV below).

C. Comparison with the virtual detector method for simulating KER spectra

In addition to the FT calculations, we also applied an alternative, the so-called “virtual detector (VD)” method for obtaining KER spectra [22]. This method allows the
FIG. 6. (Color online) Calculated KER spectra for the dipole-coupled states \( a^4\Pi_u \) and \( f^4\Pi_g \) as a function of pump-probe delay for (a) \( R_1 = 3 \), (b) 4, (c) 4.5, and (d) 5 for a 10 fs, \( 3 \times 10^{14} \) W/cm\(^2\) probe laser pulse.

computation of fragment-momentum distributions without propagating the wave packet over a large \( R \) interval. In these VD calculations only, we used a grid length of \( R_{\text{max}} = 40 \) with spacing \( \Delta R = 0.01 \) (Fig. 7). The VD covers the \( R \) interval \([R_{\text{VD}, \text{min}}, R_{\text{VD}, \text{max}}]=[6.5,16.5]\). The calculation was carried out for a total propagation time of 800 fs with time steps of \( \Delta t = 1 \). Applying the VD method, we calculated the momentum expectation value of the fragments \( p(t_i) \) in \([R_{\text{VD}, \text{min}}, R_{\text{VD}, \text{max}}]\) at time step \( t_i \). We then combined fragment momenta that fall into small momentum bins in a histogram. From this histogram we obtained the KER spectrum (see [22] for more details). The KER spectrum obtained with the VD method in Fig. 8 is almost identical with our results obtained using the FT method for \( R_1 = 4.5 \) [Fig. 6(c)].

**D. Influence of a probe-pulse pedestal**

Figure 9 shows calculated KER spectra for the same laser parameters as in Fig. 8 using the FT method, with the exception that \( R_1 = 4 \) and a long Gaussian pedestal [12], with a length of 100 fs and peak intensity \( 5 \times 10^{11} \) W/cm\(^2\), is added to the main pulse (Fig. 10). Due to the long pedestal a prominent energy-dependent structure appears in the KER spectra. The reason why the energy-dependent structure is present only if a long pedestal is included can be explained based on the relation \( \delta E \delta t \geq \hbar \). If only short pulses are present, the resolution in energy is such that one cannot observe the energy-dependent structure. On the other hand, if only the pedestal of the probe pulse is present, the oscillatory motion cannot be resolved [7]. For example, in order to resolve energies up to 0.1 eV, corresponding to the vibrational energy spacing in the \( a^4\Pi_u \) state, one needs to use pulses that are longer than 45 fs. The time-dependent structure is due to the periodic motion of the coherent vibrational wave packet on the given \( \text{O}_2^+ \) state (the oscillation period for the \( a^4\Pi_u \) state is 33 fs; Table I). A fragment-kinetic-energy-dependent structure in the KER spectra was predicted as being due to photoionization of vibrational states [7,20].

**IV. COMPARISON WITH EXPERIMENT**

The calculated KER (14) as a function of the delay and the corresponding power spectrum (16) as a function of the QB frequency \( f \) for the \( a^4\Pi_u \)-\( f^4\Pi_g \) two-state calculation...
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are shown in Figs. 11(a) and 11(b) for a 10 fs probe pulse with a peak intensity of $3 \times 10^{14}$ W/cm$^2$ and a 100 fs, $5 \times 10^{13}$ W/cm$^2$ Gaussian probe-pulse pedestal. Figures 11(c) and 11(d) show the measured KER and power spectrum for a pump-probe intensity of $3 \times 10^{14}$ W/cm$^2$ and a pulse duration of 10 fs. The sampling time in the experimental spectrum in Fig. 11(d) is $T = 2000$ fs; the revival time (not shown) 1200 fs [7]. Comparison with the experimental results in Figs. 11(c) and 11(d) shows that several features of the experimental data are reproduced. The oscillatory structure, with a period near 33 fs, is similar to the experimental period near 34 fs. The progressive tilt in the KER with increasing delay complies with a slightly larger return time of the more energetic spectral components of the vibrational wave packet and was noticed earlier in the fragmentation of $D_2^+$ [3,13,14,23] and $O_2^+$ [7]: a nuclear wave packet with dominant spectral contribution from low-lying vibrational states oscillates faster than a vibrationally warmer wave packet (corresponding to higher KER), causing the KER structure to tilt toward larger delays for larger KERs. The difference in the classical oscillation periods [24] that correspond to wave-packet components centered around $\nu = 11$ and 13 vibrational states amounts to $\sim 2.5$ fs. This is consistent with the oscillation period difference between the peaks on energy cuts at 0.13 and 0.32 eV in the calculated KER spectra. However, the same difference in oscillation periods is obtained from the measured data for 0.14 and 0.25 eV.

For better comparison with the measured KER we focal-volume averaged our calculations for the intensity range $10^{13}$ to $4 \times 10^{14}$ W/cm$^2$ with steps of $10^{13}$ W/cm$^2$, keeping the ratio between the peak intensities of the main pulse and the pedestal constant, according to

$$C_{\text{diss}}(E, \tau) = \frac{1}{N} \sum_{n=1}^{N} C_{\text{diss}}(I_n; E, \tau),$$

where $C_{\text{diss}}$ is given by (14) (Fig. 12). The volume-averaging effect on the energy-dependent structure is small. As in Figs. 9 and 11(a), the energy-dependent structure, with a spacing of approximately 0.1 eV, is still seen in the focal-volume-averaged result [Fig. 12(b)], where the separation between the peaks corresponds to the kinetic energies from the vibrational states in the $a ^4\Pi_u$ electronic state: $\nu = 10$ (0.03 eV), $\nu = 11$ (0.13 eV), $\nu = 12$ (0.23 eV), $\nu = 13$ (0.32 eV), and $\nu = 14$ (0.41 eV). The expected KERs in the brackets are calculated as the dissociation energy limit of the $a ^4\Pi_u$ state subtracted from the sum of the given vibrational level and photon energy. The vibrational state $\nu = 10$ of the $a ^4\Pi_u$ state is energetically just above the dissociation limit of the $f^4\Pi_2-\omega$ field-dressed Floquet potential-energy curve. Fig. 12(a) shows the Franck-Condon amplitudes $|a_\nu|^2$ for vertical ionization. The population decreases as the vibrational quantum number increases. Thus, we conclude that the origin of the energy structure likely arises from the vibrational states as predicted in Refs. [7,20].

V. SUMMARY

We developed a method for identifying the adiabatic electronic states involved in the dissociation of small molecules. We first calculated adiabatic potential curves and electric dipole-coupling matrix elements with the quantum chemistry code GAMESS. Next, we calculated nuclear probability-density spectra as a function of time and QB frequency for one molecular potential curve at a time and compared calculated
revival times and beat frequencies with experimental data. After identifying relevant electronic states, we included laser-induced dipole coupling in improved wave-packet propagation calculations and again compared resulting KER spectra with experimental data [7]. We applied this scheme to O2 molecules. After separately employing different combinations of electronic states of O2+ in our calculations, we concluded that the a 4Πu and f 4Πg states are key players in the dissociation dynamics, as the calculated and measured KER are similar, with matching oscillation periods and revival times (not shown in Fig. 11).

Calculating KER spectra in nuclear wave-packet propagation calculations based on the Fourier-transformation method discussed in Sec. III B and the virtual detector method in Sec. III C, we obtained almost identical results. KER calculations including long probe-pulse pedestals were found to add an energy-dependent structure that is reminiscent of - but does not clearly reproduce - the energy dependence in measured KER spectra. The interpretation of this observed energy dependence remains a challenge for future investigations.

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APPENDIX

1. Choice of basis functions

Atomic orbitals (AO) are modeled as Gaussian functions centered at each nuclei of the diatomic molecule (or molecular ion). These AO orbitals are linearly combined to form MOs with a set of expansion coefficients \{C_i\}. The MOs are multiplied with electron-spin orbitals and combined to make Slater determinants in order to satisfy the Pauli exclusion principle. The CSF wave functions are equivalent to these Slater determinants (once the coefficients \{C_i\} have been optimized). The CSF wave functions are linearly combined to create the MC wave function with coefficients \{A_k\}. The expansion coefficients \{C_i\} and \{A_k\} are determined simultaneously based on a variational principle [11].

The appropriate choice of basis functions is important for the accuracy of the calculated potential curves. The basis set is the set of (mathematical) functions (for example Gaussians) from which the WF is constructed. Since HF and MCSCF methods are variational, larger basis sets usually lead to more accurate results. The basis set with two Gaussians on each AO is called a “double-ζ” basis. The higher the number of Gaussians used for each AO is, the more complete the basis is (multiple-ζ basis set). We used the Dunning-type correlation-consistent polarized valence triple-ζ basis set (cc-pVTZ) [25]. The Dunning-type basis set is an example of a multiple-ζ basis set. The correlation-consistent part of the name indicates that the basis set was optimized for calculations including electron correlation through excited CSFs.

2. Configuration state wave functions

The MCSCF WFs were optimized with the \([f(1σ_g)^2(1σ_u)^2(2σ_g)^2(2σ_u)^2)^4] \) “frozen core,” meaning that the occupations of those MOs were not allowed to vary. The calculations were done for fixed internuclear separations R with steps of 0.02 Å. Dipole-coupling matrix elements for different R were calculated including configuration interaction within the graphical unitary group approach (GUGA) [26].

The ground state of the oxygen molecule has the configuration \([f(1σ_g)^2(1σ_u)^2(2σ_g)^2(2σ_u)^2)^4]3σ_g^2(1π_u)^1(1π_g)^1\). A large number of final molecular ion states with different multiplicities and symmetries can be generated after valence photoionization. Some of these states are given in Table II, which shows the main configurations that contribute more than 70% to the norm of the MCSCF WF. GAMES outputs only designate electronic configurations. To link the calculated potential curves and dipole-coupling matrix elements to a given MCSCF state, we used Table II.

The MCSCF process minimizes energy using the variational principle. “Root switching” can be a problem if two states are close in energy and MO and CSF coefficients are only optimized for one MCSCF state. To avoid this problem, we carried out state-averaged MCSCF calculations [27], where MO orbitals are optimized not for any one state energy \(E_j\) (which is usually the ground state), but for the average of two or more states \(\bar{E} = \sum_{j}^N w_j E_j\), where \(N\) is the number of states (in our case 14) included in the average and the coefficients \(w_j\) are positive constants with normalization \(\sum_j w_j = 1\). The MCSCF WFs are optimized to minimize the energies \(E_j\). The number of MOs used in the variation space was 60; the number of the Cartesian Gaussian basis functions (atomic orbitals) used was 70. In MCSCF calculations, the specification of how many MO are occupied is crucial. One needs to specify the so-called active space. MCSCF active-space choices are often abbreviated as “(m,n),” where \(m\) is the number of active electrons and \(n\) is the number of orbitals. As an active space we used MCSCF (7, 6) for O2+. The six orbitals are the \(σ, π, σ^*, π^*\) orbitals of O2.

3. Geometry optimizations

When performing computations, it is important to understand the geometry of the molecule since many of the physical and chemical properties of the molecule depend on it. We optimized the molecular geometry of neutral (equilibrium internuclear distance of 1.152 Å) and singly charged (equilibrium internuclear distance of 1.087 Å) oxygen.
molecules using restricted open-shell SCF WFs, where the occupation of closed shells by the electrons is assumed to be fixed, with the WFs represented as a single Slater determinant. “Restricted” indicates that the spin-up and spin-down orbital coefficients in the expansion and energies are the same. The symmetry used was \(D_4h\) for the linear molecule with inversion center [28] since the full \(D_\infty h\) point group is not supported in GAMESS.