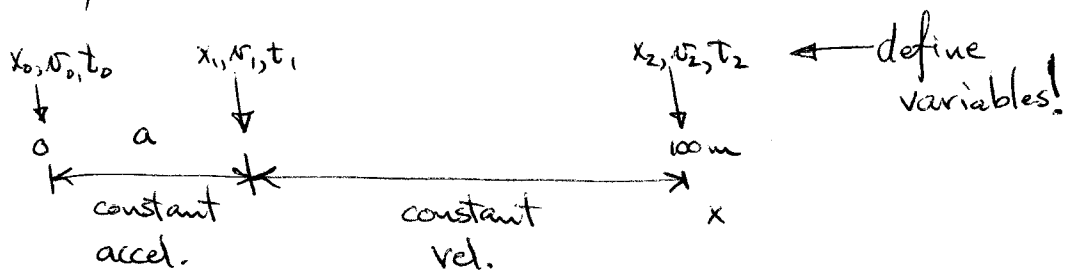


Since we didn't get to do any examples in lecture, let me answer this in more detail.

First, let's try to sketch the situation:



Next, what do we know?

> Total time, t_2

> Time for acceleration, t_1

> Total distance, x_2

> Initial conditions, $x_0=0, v_0=0, t_0=0$.

> $v_2 = v_1$

What don't we know?

> x_1 or v_1

> a , of course!

Since there were two parts to the race, part with acceleration and part without, it ~~makes sense~~ we should break our analysis into two pieces:

$$\underline{0 \leq t \leq t_1} \quad x_1 = x_0 + v_0 t_1 + \frac{1}{2} a t_1^2$$

$$v_1 = v_0 + a t_1$$

$$\underline{t_1 \leq t \leq t_2} \quad x_2 = x_1 + v_1 (t_2 - t_1)$$

Now we have

$$x_1 = \frac{1}{2}at_1^2$$

$$v_1 = at_1$$

$$x_2 = x_1 + v_1(t_2 - t_1)$$

⇒ 3 equations with 3 unknowns!

So, we can solve for the unknown we're interested in, a , in terms of known quantities.

Explicitly, eliminating x_1 & v_1 :

$$x_2 = \frac{1}{2}at_1^2 + at_1(t_2 - t_1)$$

$$x_2 = at_1(t_2 - \frac{1}{2}t_1)$$

or

$$a = \frac{x_2}{t_1(t_2 - \frac{1}{2}t_1)}$$

← at this point only do we substitute numerical values!

Note that I've deliberately been very wordy here so that the logic is (hopefully!) transparent.

The strategy I have employed is pretty general — and it follows the strategy outlined in the syllabus and text (Picture, Solve, Check).

To complete this as an example, I show below the x vs t and v vs t plots for this problem!

