## Attosecond and strong field physics C. D. Lin, Anh Thu Le, Cheng Jin and Hui Wei (Cambridge University Press 2018)

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