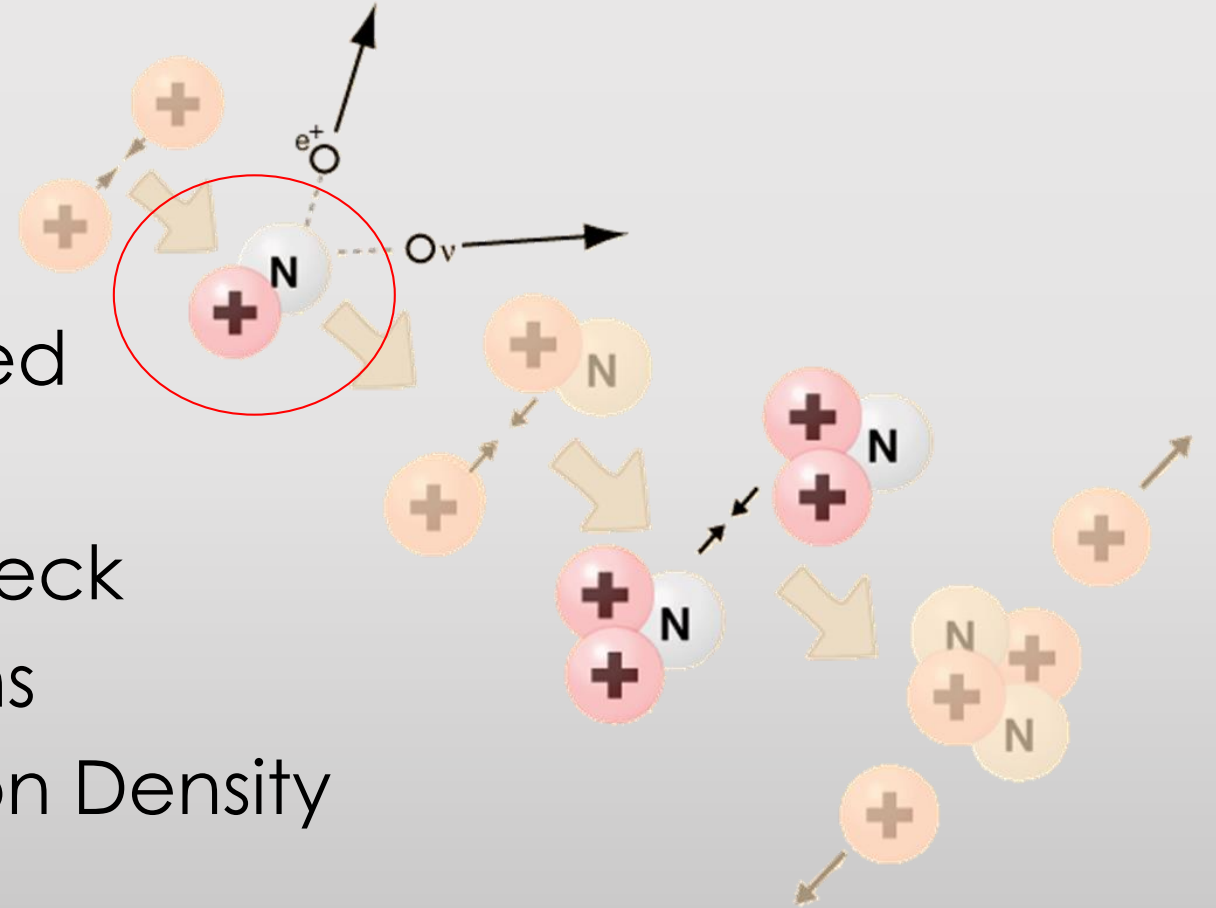


# Analysis of Deuterium Abundance

Jacob Peyton, Jarred Penton, Aasim Zahoor, Bharat Ratra

# Big Bang Nucleosynthesis

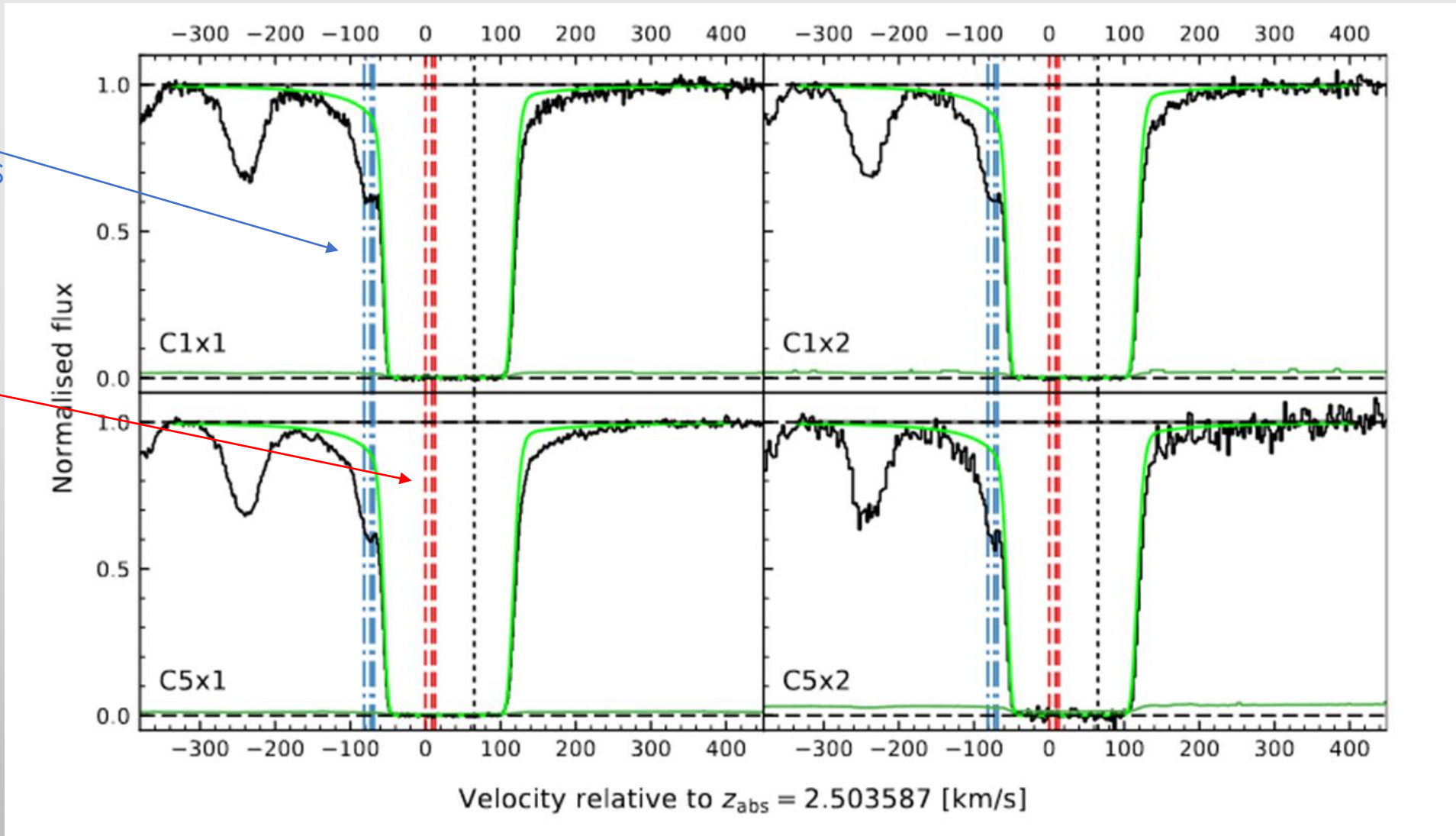
- Hydrogen to Lithium Produced
- Fusion Lasted For 20 Minutes
- Deuterium is a Fusion Bottleneck
- Lightest Isotope with Neutrons
- Production Sensitive to Baryon Density



# Spectroscopy

Deuterium  
Lyman Lines

Hydrogen  
Lyman Lines



# Zavarygin et al's Results

$$(D/H)_p = (2.545 \pm 0.025) \times 10^{-5}$$

$$\Omega_b h^2 = 0.02174 \pm 0.00025$$

Quasar	D/H( $\times 10^5$ )	Reference
HS 0105+1619	$2.58^{+0.16}_{-0.15}$	Cooke et al. (2014)
J0407-4410	$2.8^{+0.8}_{-0.6}$	Noterdaeme et al. (2012)
Q0913+72	$2.53^{+0.11}_{-0.10}$	Cooke et al. (2014)
Q1009+2956	$2.48^{+0.41}_{-0.13}$	Zavarygin et al. (2018)
J1134+5742	$2.0^{+0.7}_{-0.5}$	Fumagalli et al. (2011)
Q1243+3047	$2.39 \pm 0.08$	Cooke et al. (2018)
J1337+3152	$1.2^{+0.5}_{-0.2}$	Srianand et al. (2010)
SDSS	$2.62 \pm 0.07$	Cooke et al. (2016)
J1358+6522	$2.58 \pm 0.07$	Cooke et al. (2014)
J1419+0829	$2.51 \pm 0.05$	Cooke et al. (2014)
J1444+2919	$1.97^{+0.33}_{-0.28}$	Balashhev et al. (2016)
J1558-0031	$2.40^{+0.15}_{-0.14}$	Cooke et al. (2014)
PKS1937-1009	$2.45^{+0.30}_{-0.27}$	Reimer-Sørensen et al. (2015)
PKS1937-101	$2.62 \pm 0.05$	Reimer-Sørensen et al. (2017)
Q2206-199	$1.65 \pm 0.35$	Pettini & Bowen (2001)

# Median Statistics

Truncated 13 Weighted Mean

$$(D/H)_p = (2.545 \pm 0.025) \times 10^{-5}$$

$$\Omega_b h^2 = 0.02174 \pm 0.00025$$

All 15 Median

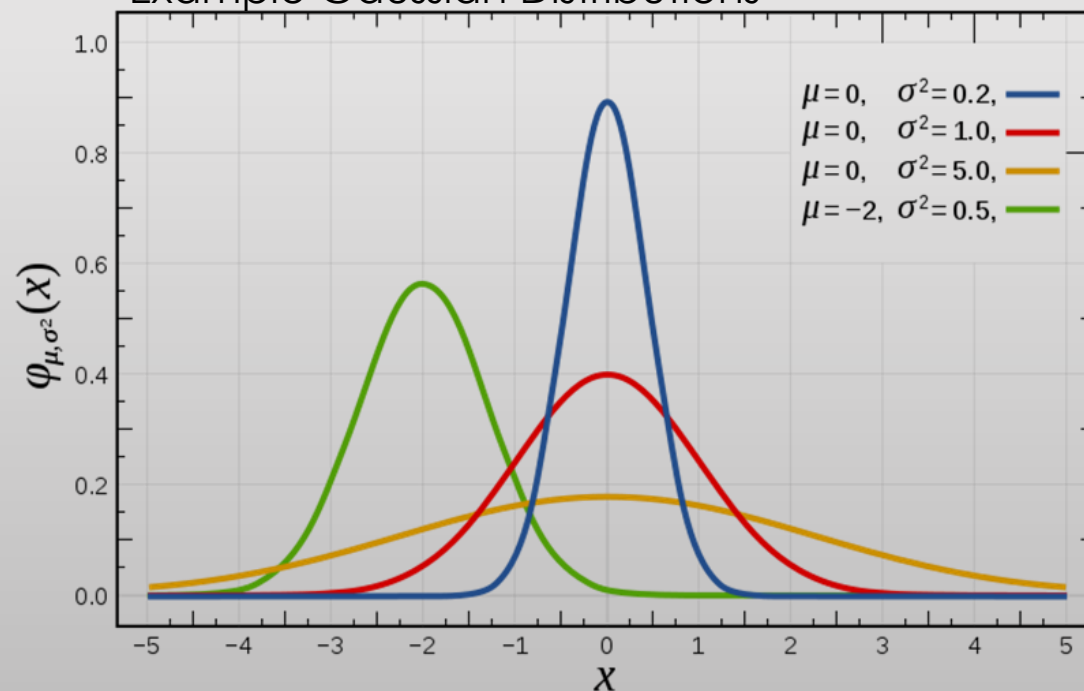
$$(D/H)_p = (2.48 \pm 0.065) \times 10^{-5}$$

$$\Omega_b h^2 = 0.02209 \pm 0.00041$$

$$P = \frac{2^{-N} N!}{i! (N - i)!}$$

$1\sigma$  ( $2\sigma$ ) at 68.27% (95.45%)

Example Gaussian Distributions



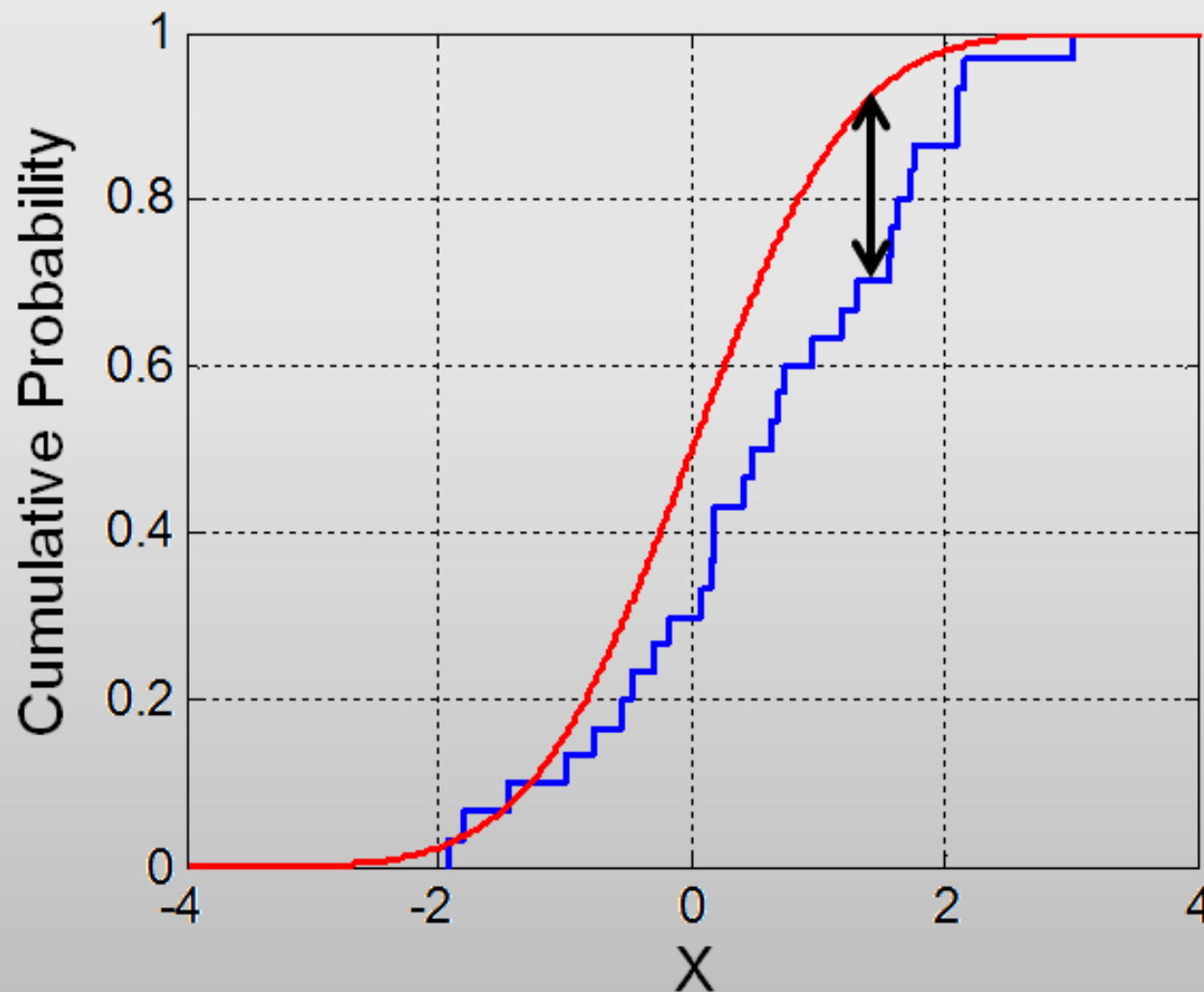
# Kolmogorov-Smirnov Test

$$Q_{KS}(z) = 2 \sum_{j=1}^{\infty} (-1)^{j-1} \exp(-2j^2 z^2)$$

$$z = (\sqrt{N} + 0.12 + 0.11/\sqrt{N}) * D$$

$$\text{Prob}(D > \text{Observed}) = Q_{KS}(z)$$

	All 15 p	Truncated 13 p
Gaussian	0.809	0.997
Cauchy	0.921	0.604



# Baryonic Density

Truncated 13 Weighted Mean

$$(D/H)_p = (2.545 \pm 0.025) \times 10^{-5}$$

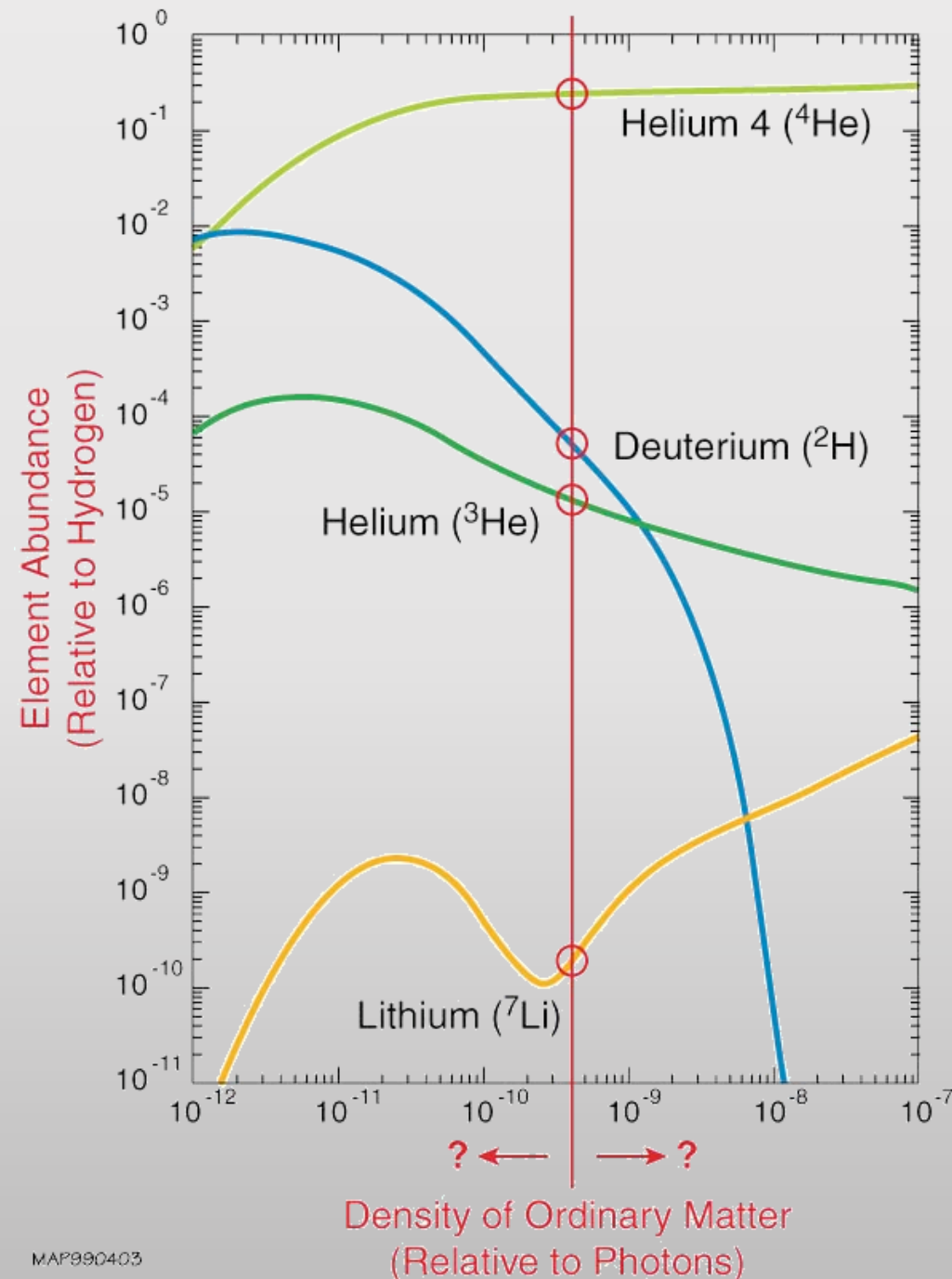
$$\Omega_b h^2 = 0.02174 \pm 0.00025$$

All 15 Median

$$(D/H)_p = (2.48 \pm 0.065) \times 10^{-5}$$

$$\Omega_b h^2 = 0.02209 \pm 0.00041$$

$$(D/H)_p = (2.45 \pm 0.04) \times 10^{-5} \left( \frac{\Omega_b h^2}{0.02225} \right)^{-1.657}$$



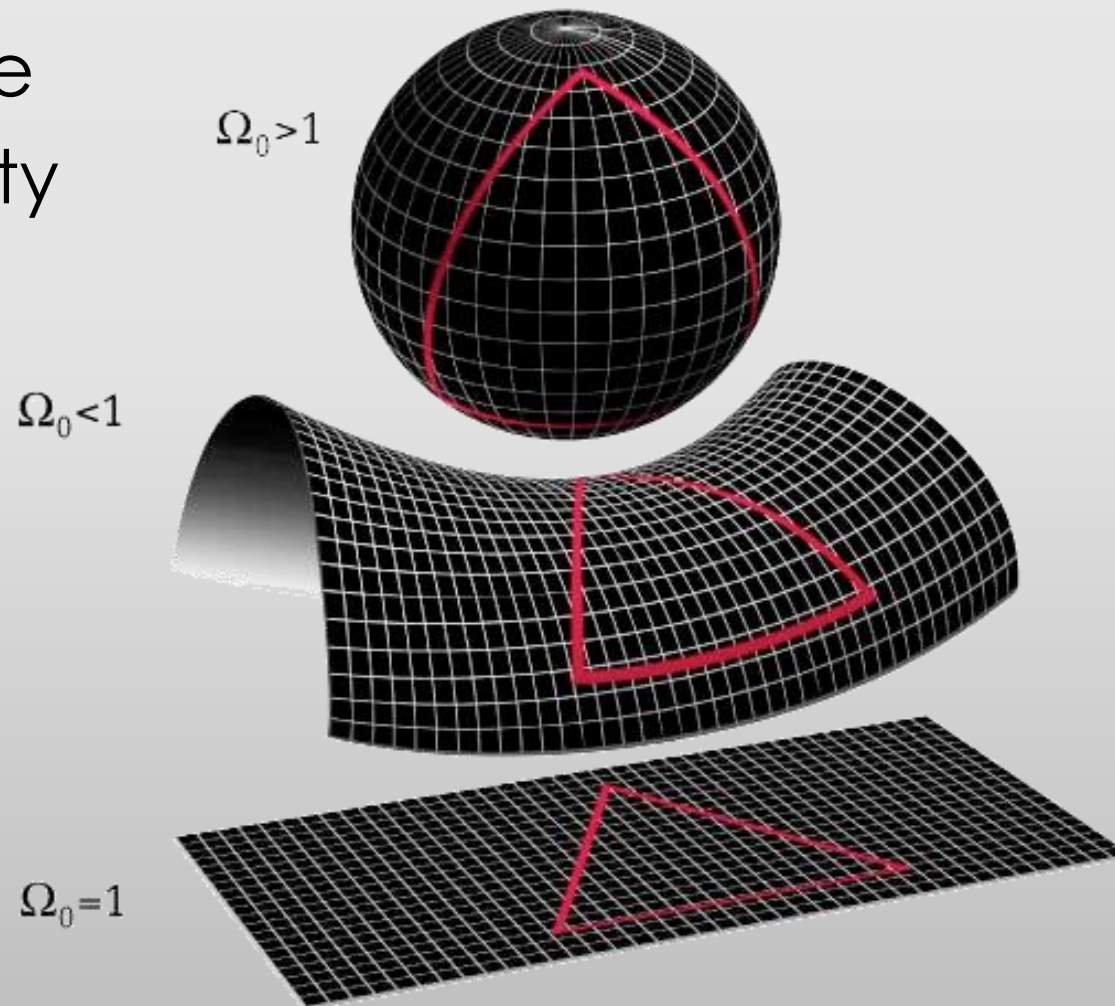
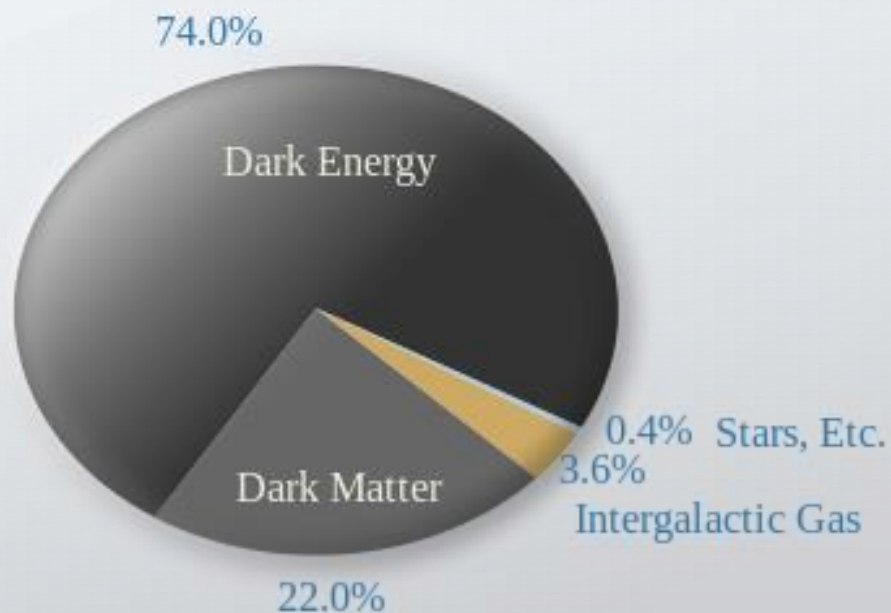
# Planck Collaboration

	CMB Data Alone			CMB and Other Data		
Cosmogony	$\Omega_b h^2$	WM $\sigma$	Median $\sigma$	$\Omega_b h^2$	WM $\sigma$	Median $\sigma$
Flat $\Lambda$ CDM	$0.0225 \pm 0.00023$	1.5	0.34	$0.02232 \pm 0.00019$	1.8	0.51
Nonflat $\Lambda$ CDM	$0.02305 \pm 0.0002$	4.1	2.1	$0.02305 \pm 0.00019$	4.1	2.1
Flat XCDM	$0.02229 \pm 0.00023$	1.6	0.43	$0.02233 \pm 0.00021$	1.8	0.52
Nonflat XCDM	$0.02305 \pm 0.0002$	4.1	2.1	$0.02305 \pm 0.0002$	4.1	2.1
Flat $\phi$ CDM	$0.02221 \pm 0.00023$	1.4	0.26	$0.02238 \pm 0.0002$	2.0	0.64
Nonflat $\phi$ CDM	$0.02303 \pm 0.0002$	4.0	2.1	$0.02304 \pm 0.0002$	4.0	2.1



# The End of the Universe

- End Determined by Curvature
- Curvature Depends on Density
- $\Omega_0 = \text{Density}/\text{Critical Density}$



# Further Research

- More Data Points
- Other Cosmological Data Sources
- Comparing More Distributions

# Acknowledgements

Jarred Penton  
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Bharat Ratra  
Tia Camarillo  
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Gott et al.



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