

## Prefixes

a=10<sup>-18</sup>, f=10<sup>-15</sup>, p=10<sup>-12</sup>, n=10<sup>-9</sup>,  $\mu = 10^{-6}$ , m=10<sup>-3</sup>, c=10<sup>-2</sup>, k=10<sup>3</sup>, M=10<sup>6</sup>, G=10<sup>9</sup>, T=10<sup>12</sup>, P=10<sup>15</sup>

## Physical Constants

$$\begin{aligned}g &= 9.80 \text{ m/s}^2 \text{ (gravitational acceleration)} \\M_E &= 5.98 \times 10^{24} \text{ kg (mass of Earth)} \\m_e &= 9.11 \times 10^{-31} \text{ kg (electron mass)} \\c &= 299792458 \text{ m/s (speed of light)} \\u &= 1.6605 \times 10^{-27} \text{ kg (atomic mass unit)} \\R &= 8.314 \text{ J/mol}\cdot\text{K (gas constant)}$$

$$\begin{aligned}G &= 6.67 \times 10^{-11} \text{ N}\cdot\text{m}^2/\text{kg}^2 \text{ (Gravitational constant)} \\R_E &= 6380 \text{ km (mean radius of Earth)} \\m_p &= 1.67 \times 10^{-27} \text{ kg (proton mass)} \\\sigma &= 5.67 \times 10^{-8} \text{ W/m}^2\cdot\text{K}^4 \text{ (Stefan-Boltzmann constant)} \\N_A &= 6.022 \times 10^{23}/\text{mol (Avogadro's number)} \\k &= 1.38 \times 10^{-23} \text{ J/K (Boltzmann's constant)}$$

## Units and Conversions

$$\begin{aligned}1 \text{ inch} &= 1 \text{ in} = 2.54 \text{ cm (exactly)} \\1 \text{ mile} &= 5280 \text{ ft} \\1 \text{ m/s} &= 3.6 \text{ km/hour} \\1 \text{ acre} &= 43560 \text{ ft}^2 = (1 \text{ mile})^2/640\end{aligned}$$

$$\begin{aligned}1 \text{ foot} &= 1 \text{ ft} = 12 \text{ in} = 30.48 \text{ cm (exactly)} \\1 \text{ mile} &= 1609.344 \text{ m} = 1.609344 \text{ km} \\1 \text{ ft/s} &= 0.6818 \text{ mile/hour} \\1 \text{ hectare} &= 10^4 \text{ m}^2\end{aligned}$$

## Some Elemental Properties

symbol	element	atomic number	mass number
H	hydrogen	1	1.00794
He	helium	2	4.00260
C	carbon	6	12.0107
N	nitrogen	7	14.0067
O	oxygen	8	15.9994
Ne	neon	10	20.180
Ar	argon	18	39.948
Fe	iron	26	55.845
Ni	nickel	28	58.693
Cu	copper	29	63.546
Au	gold	79	196.97
U	uranium	92	238.03

Mass numbers are atomic masses in units of “u” where  $1 \text{ u} = 1.6605 \times 10^{-27} \text{ kg}$ , or, molar masses for the element ( $1 \text{ mole} = 6.02 \times 10^{23} \text{ atoms}$ ), measured in grams. ( $N_A \times 1 \text{ u} = 1 \text{ gram}$ )

## Trig summary

$$\begin{aligned}\sin \theta &= \frac{(\text{opp})}{(\text{hyp})}, & \cos \theta &= \frac{(\text{adj})}{(\text{hyp})}, & \tan \theta &= \frac{(\text{opp})}{(\text{adj})}, & (\text{opp})^2 + (\text{adj})^2 &= (\text{hyp})^2. \\ \sin \theta &= \sin(180^\circ - \theta), & \cos \theta &= \cos(-\theta), & \tan \theta &= \tan(180^\circ + \theta), & \sin^2 \theta + \cos^2 \theta &= 1.\end{aligned}$$

## Vectors

Written  $\vec{V}$  or  $\mathbf{V}$ , described by magnitude= $V$ , direction= $\theta$  or by components  $(V_x, V_y)$ .

$$V_x = V \cos \theta, \quad V_y = V \sin \theta,$$

$$V = \sqrt{V_x^2 + V_y^2}, \quad \tan \theta = \frac{V_y}{V_x}. \quad \theta \text{ is the angle from } \vec{V} \text{ to } x\text{-axis.}$$

Addition:  $\mathbf{A} + \mathbf{B}$ , head to tail.

Subtraction:  $\mathbf{A} - \mathbf{B}$  is  $\mathbf{A} + (-\mathbf{B})$ ,  $-\mathbf{B}$  is  $\mathbf{B}$  reversed.

## Energy, Force, Power

Work & Kinetic & Potential Energies:

$$W = Fd \cos \theta, \quad \text{KE} = \frac{1}{2}mv^2, \quad \text{PE}_{\text{gravity}} = mgy, \quad \text{PE}_{\text{spring}} = \frac{1}{2}kx^2. \quad \theta = \text{angle btwn } \vec{F} \text{ and } \vec{d}.$$

Conservation or Transformation of Energy:

**Work-KE theorem:**

$$\Delta \text{KE} = W_{\text{net}} = \text{work of all forces.}$$

Power:

$$P_{\text{ave}} = \frac{W}{t}, \quad \text{or use } P_{\text{ave}} = \frac{\text{energy}}{\text{time}}.$$

**General energy-conservation law:**

$$\Delta \text{KE} + \Delta \text{PE} = W_{\text{NC}} = \text{work of non-conservative forces.}$$

## Fluids

Density:

$$\rho = m/V, \quad SG = \rho/\rho_{H_2O}, \quad \rho_{H_2O} = 1000 \text{ kg/m}^3 = 1.00 \text{ g/cm}^3 \text{ (at } 4^\circ\text{C)}.$$

Static Fluids:

$$P = F/A, \quad P_2 = P_1 + \rho gh, \quad \Delta P = \rho gh, \quad P = P_{\text{atm.}} + P_G, \quad B = \rho gV \text{ or } F_B = \rho gV.$$

Pressure Units:

$$1 \text{ Pa} = 1 \text{ N/m}^2, \quad 1 \text{ bar} = 10^5 \text{ Pa} = 100 \text{ kPa}, \quad 1 \text{ mm-Hg} = 133.3 \text{ Pa}.$$

$$1.00 \text{ atm} = 101.3 \text{ kPa} = 1.013 \text{ bar} = 760 \text{ torr} = 760 \text{ mm-Hg} = 14.7 \text{ lb/in}^2.$$

Moving Fluids:

$$A_1 v_1 = A_2 v_2 = \text{a constant}, \quad P + \frac{1}{2} \rho v^2 + \rho gy = \text{a constant}.$$

## Chapter 13 Equations

Atomic Theory & Moles:

$$n = \frac{N}{N_A}, \quad n = \frac{m}{M_A}, \quad N_A = 6.022 \times 10^{23}/\text{mol}, \quad 1 \text{ u} = \frac{1 \text{ gram}}{N_A} = 1.6605 \times 10^{-27} \text{ kg}.$$

Temperature scales:

$$T(\text{C}) = \frac{5}{9}[T(\text{F}) - 32], \quad T(\text{F}) = \frac{9}{5}T(\text{C}) + 32, \quad T(\text{K}) = T(\text{C}) + 273.15$$

Thermal Expansion:

$$\Delta L = \alpha L_0 \Delta T, \quad \Delta V = \beta V_0 \Delta T.$$

Ideal Gas Law:

$$PV = nRT, \quad \text{or} \quad PV = NkT, \quad R = 8.314 \text{ J/mol}\cdot\text{K}, \quad k = \frac{R}{N_A} = 1.38 \times 10^{-23} \text{ J/K}.$$

Kinetic Theory:

$$\overline{\text{KE}} = \frac{1}{2}mv_{\text{rms}}^2 = \frac{3}{2}kT, \quad v_{\text{rms}} = \sqrt{\frac{3kT}{m}} = \sqrt{\frac{3RT}{M_A}}, \quad m = M_A/N_A.$$

## Chapter 14 Equations

Internal Energy:

$$U = \frac{3}{2}NkT = \frac{3}{2}nRT, \quad \text{for ideal monatomic gases.}$$

Mechanical Equivalent of Heat, Specific Heat, Latent Heat:

$$1 \text{ cal} = 4.186 \text{ J}, \quad Q = mc\Delta T, \quad Q = mL_F, \quad Q = mL_V.$$

For water,  $c = 1.00 \text{ cal/g}\cdot\text{C}^\circ = 4.186 \text{ kJ/kg}\cdot\text{C}^\circ$ ,  $c_{\text{ice}} = 0.50 \text{ cal/g}\cdot\text{C}^\circ = 2.1 \text{ kJ/kg}\cdot\text{C}^\circ$ .

$$L_F = 79.7 \text{ kcal/kg} = 333 \text{ kJ/kg}, \quad L_V = 539 \text{ kcal/kg} = 2260 \text{ kJ/kg}.$$

Heat Transfer:

$$\text{Conduction: } P = \frac{Q}{t} = kA\frac{\Delta T}{l}.$$

$$\text{Radiation: } P = \frac{\Delta Q}{\Delta t} = e\sigma AT^4, \quad P = \frac{\Delta Q}{\Delta t} = e\sigma A(T_1^4 - T_2^4), \quad \sigma = 5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4.$$

$$\text{Solar Energy: } P = \frac{\Delta Q}{\Delta t} \approx (1000 \text{ W/m}^2) eA \cos \theta$$

## Chapter 15 Equations

First Law of Thermodynamics ( $U$  = internal energy):

$$\Delta U = Q - W \quad \text{or} \quad \Delta KE + \Delta PE + \Delta U = Q - W$$

work =  $W$  = area under  $P(V)$  curve.  $W = P\Delta V$  for isobaric processes.

heat =  $Q$  = heat absorbed by the system.  $Q = 0$  for adiabatic processes.

Heat Engines:

$$W = Q_H - Q_L, \quad \text{efficiency } e = \frac{W}{Q_H} = 1 - \frac{Q_L}{Q_H}, \quad \frac{Q_L}{Q_H} = \frac{T_L}{T_H} \text{ for ideal Carnot cycle.}$$

Cooling Machines, Heat Pumps:

$$W = Q_H - Q_L, \quad \text{refrigerators: } \text{COP} = \frac{Q_L}{W}, \quad \text{heat pumps: } \text{COP} = \frac{Q_H}{W}, \quad \frac{Q_L}{Q_H} = \frac{T_L}{T_H} \text{ for ideal Carnot.}$$

Power:

$$P_{\text{ave}} = \frac{W}{t}, \quad \text{or use } P_{\text{ave}} = \frac{\text{energy}}{\text{time}}.$$